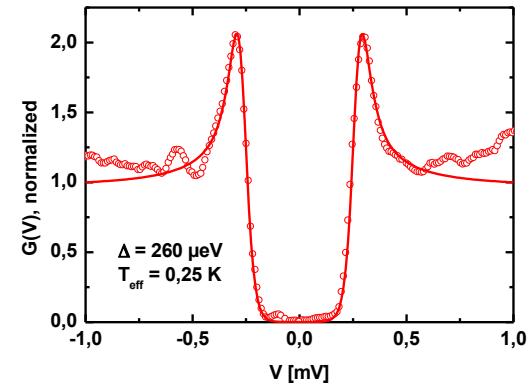
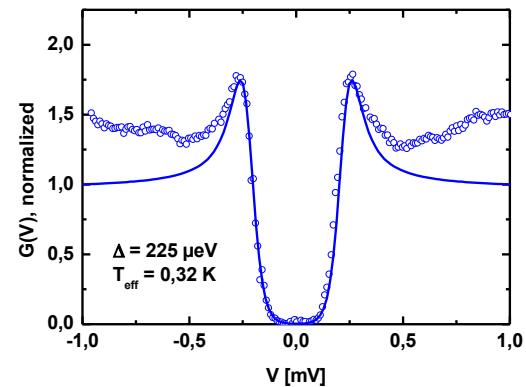
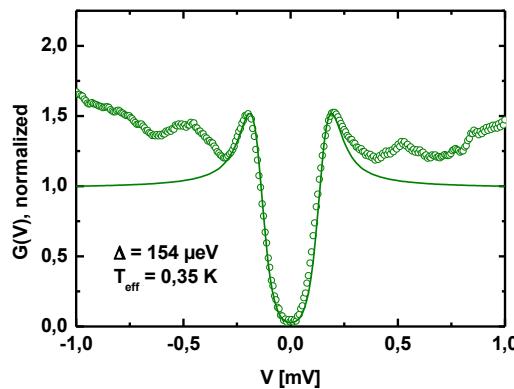
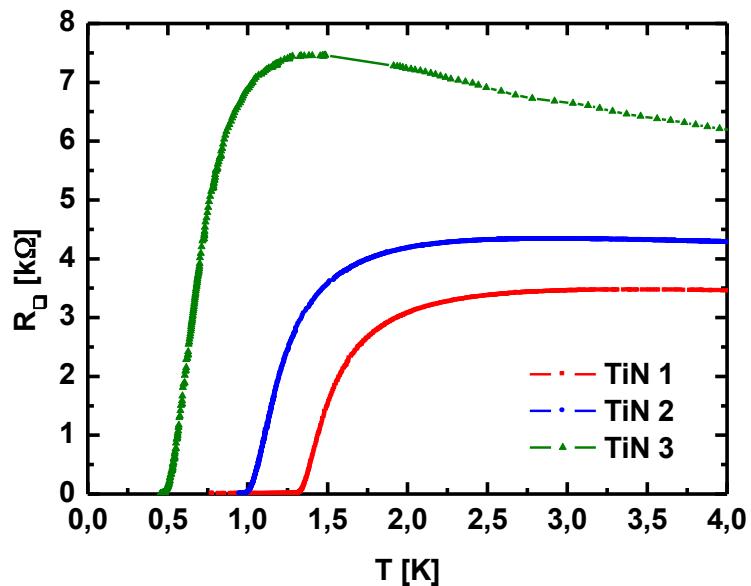
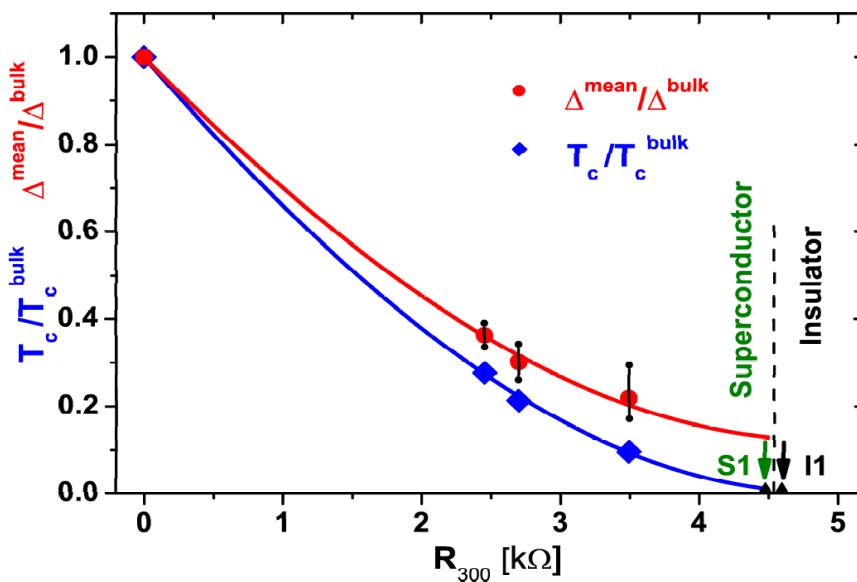
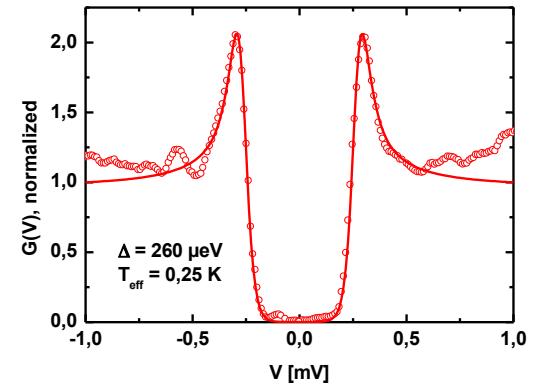
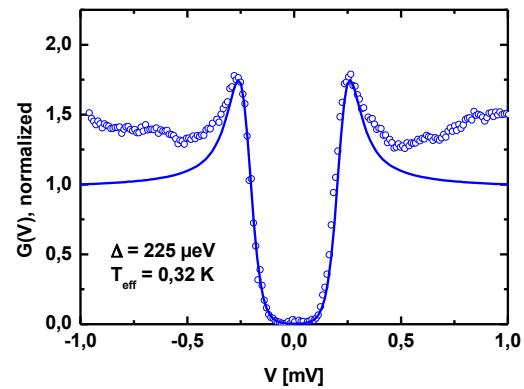
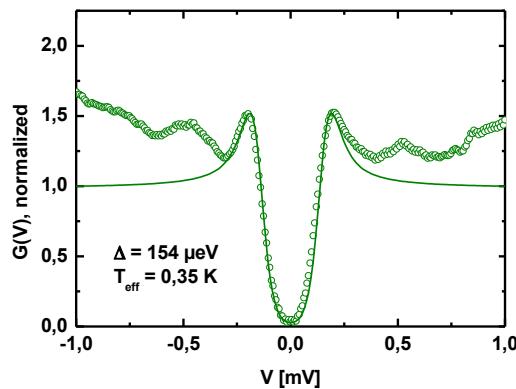
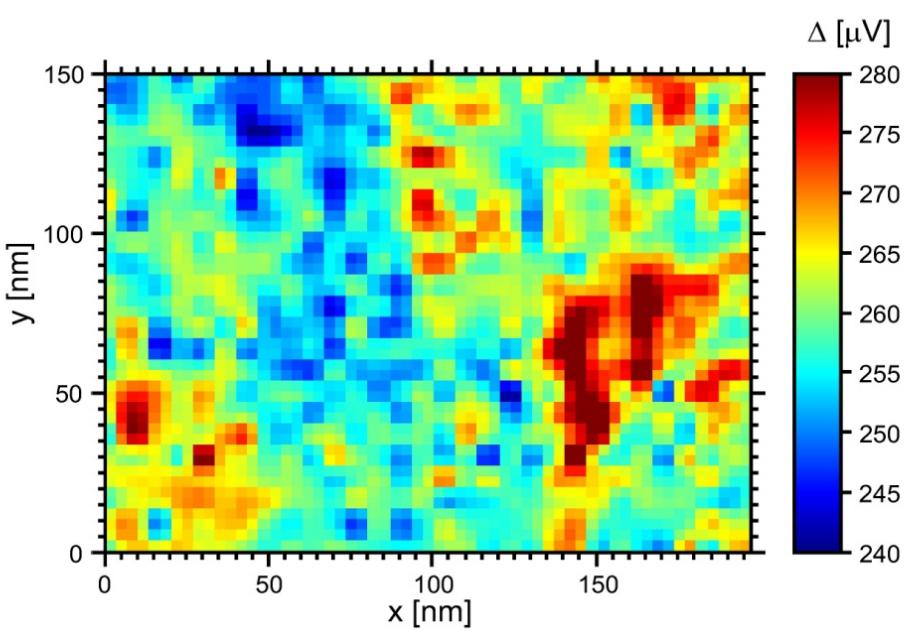
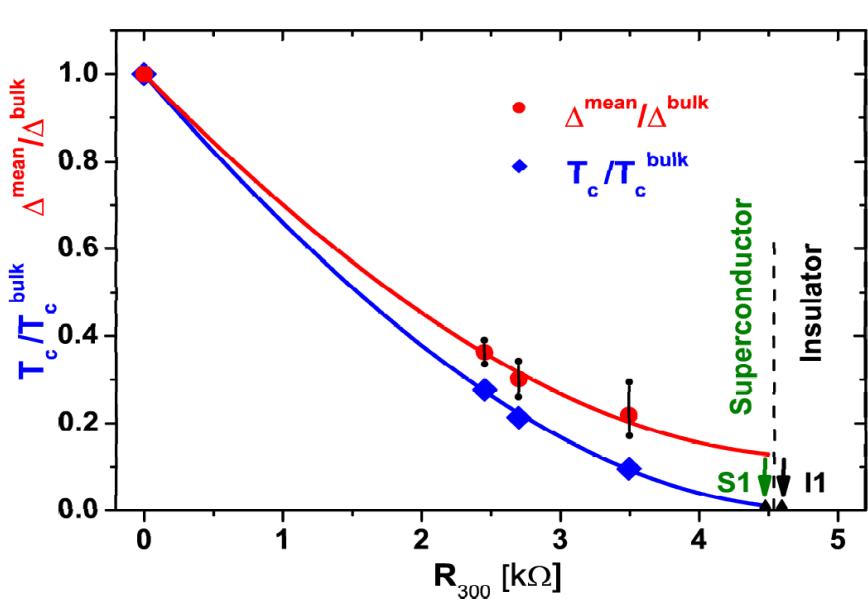


TIN Superconductor-Insulator transition



Increasing disorder

TIN Superconductor-Insulator transition

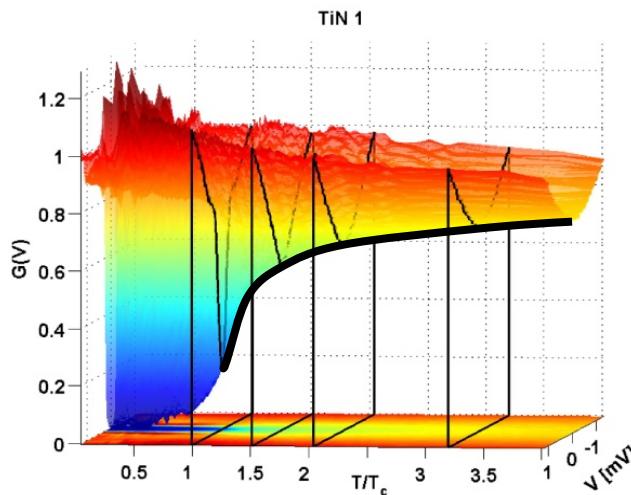
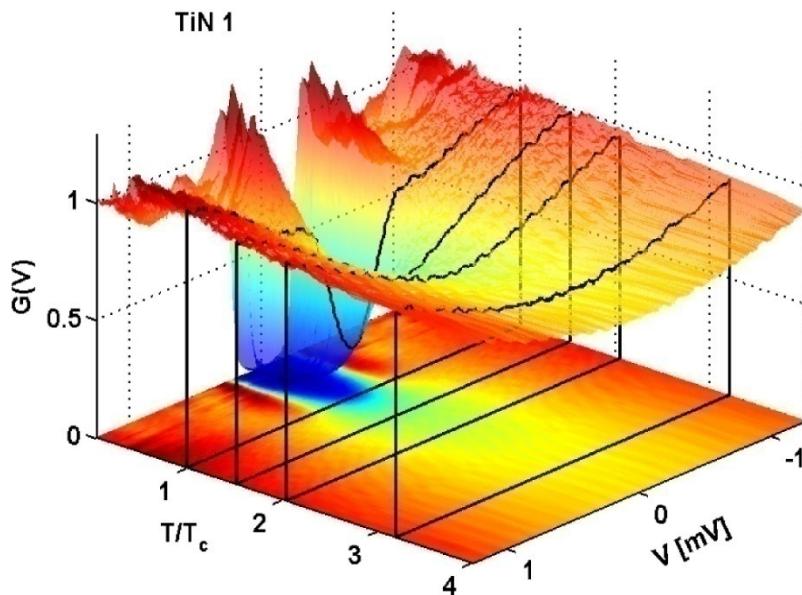


Increasing disorder

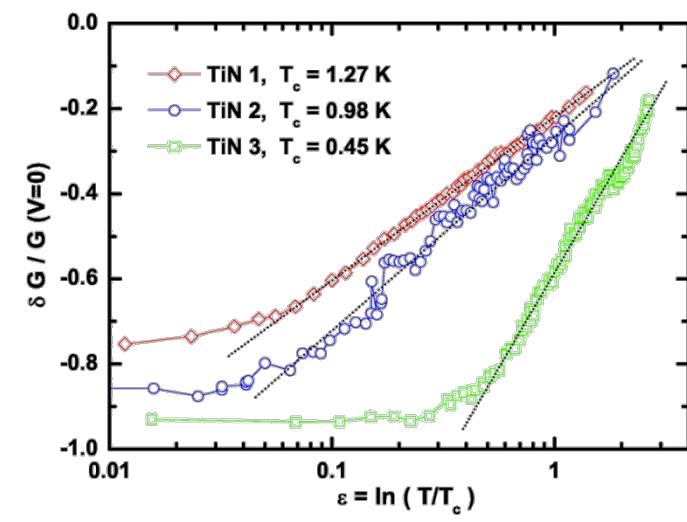
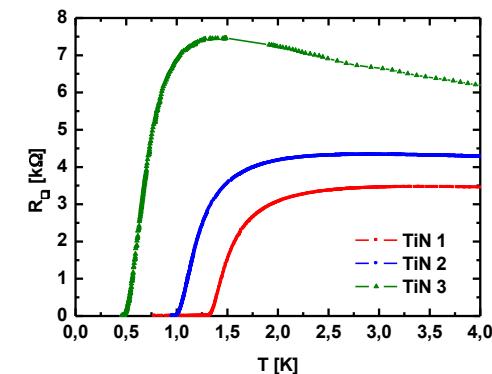
Pseudogap

Superconducting fluctuations correction to the DOS

Preformed Cooper pairs above T_c



B. Sacépé, et al., Nature Communications (2010)



$$\frac{\delta G}{G}(eV = 0) = -2Gi \ln(\ln \frac{T}{T_c})$$

A. Varlamov and V. Dorin, Sov. Phys. JETP 57, 1089, (1983)

Localization of preformed Cooper pairs in highly disordered superconducting films

Thomas Dubouchet, Benjamin Sacépé, Marc Sanquer, Claude Chapelier
INAC-SPSMS-LaTEQS, CEA-Grenoble

T. Baturina, *Institute of semiconductor Physics - Novosibirsk*

V. Vinokur, *Material Science Division, Argonne National Laboratory - Argonne*

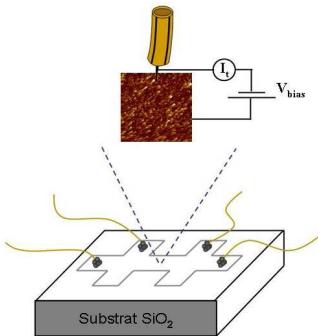
M. Baklanov, A Satta, *IMEC - Leuven*

Maoz Ovadia, Dan Shahar, *The Weizmann Institute of Science*

Mikhail Feigel'man, *L. D. Landau Institute for Theoretical Physics*

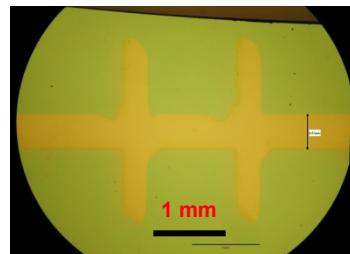
Lev Ioffe, *Serin Physics laboratory, Rutgers University*

Amorphous Indium Oxide

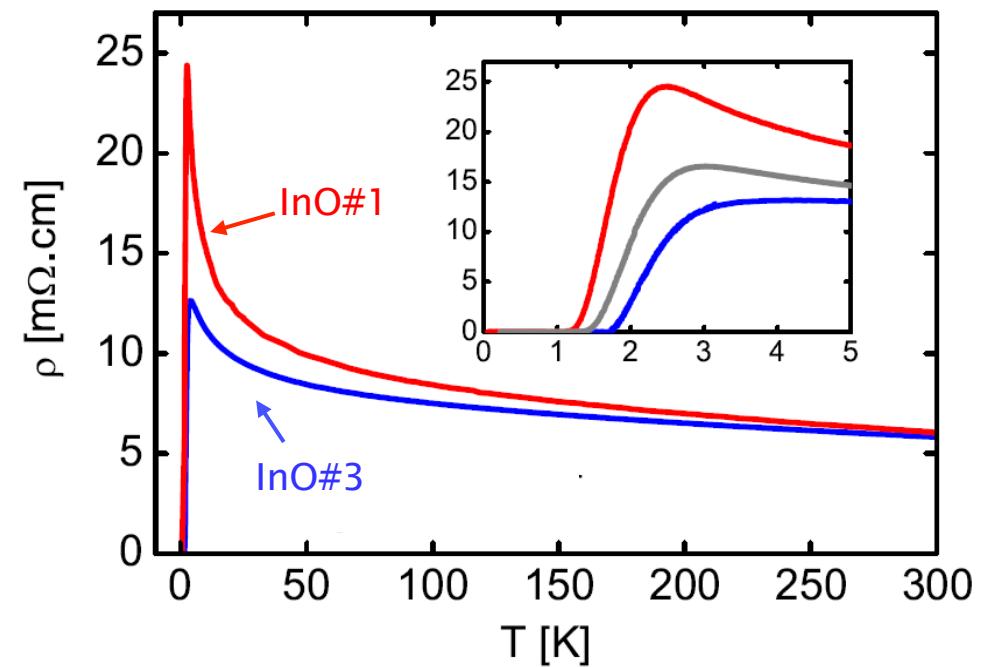
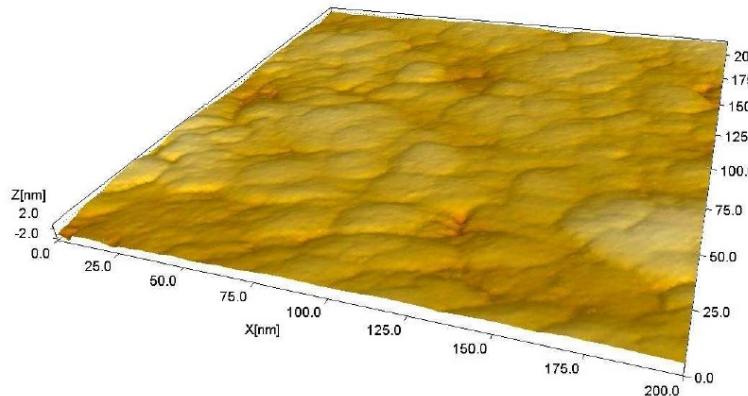


Samples: e-gun evaporation of high purity In_2O_3 onto Si/SiO₂ substrate under O₂ pressure

D. Shahar, Weizmann Institute of Science

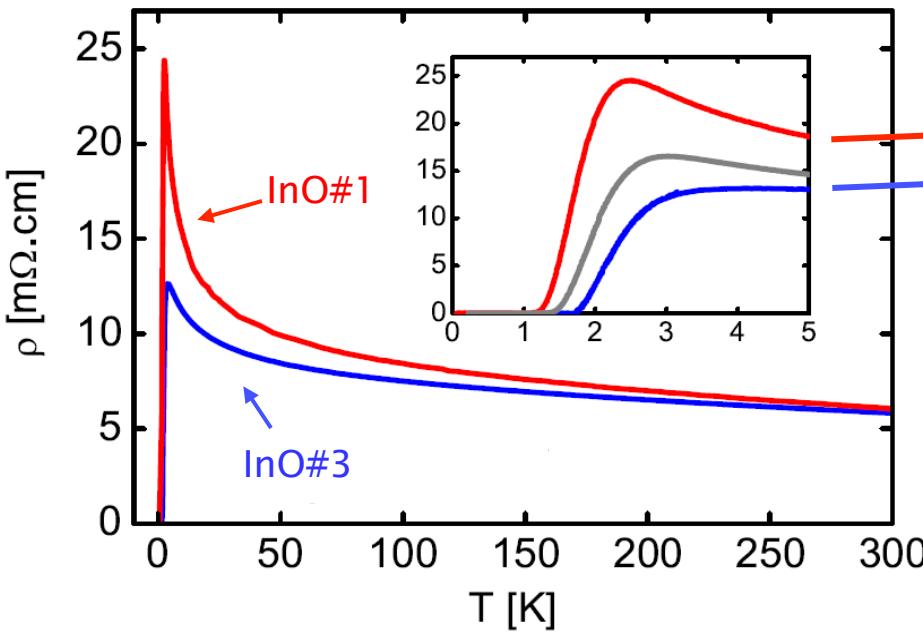


Thickness : 15 nm (red & grey) and 30 nm (blue) – 3D regime

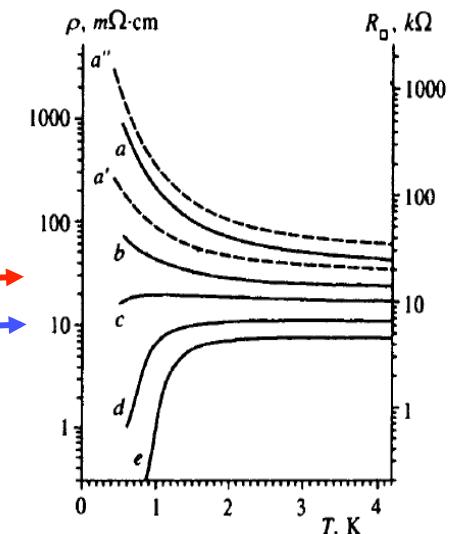


Nearly critical samples

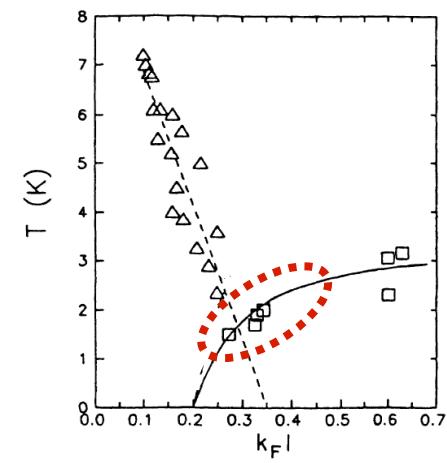
High disorder (red) and low disorder (blue)



- $k_F l_e \sim 0.4\text{-}0.5 < 1 \rightarrow$ localized regime (Ioffe-Regel criterion)
- T_c comprised between 1K and 2K
- Carrier density : $N = 3.5 \times 10^{21} \text{ cm}^{-3}$

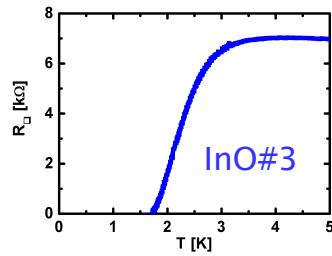


V. F. Gantmakher et al., JETP 82, 951 (1996)

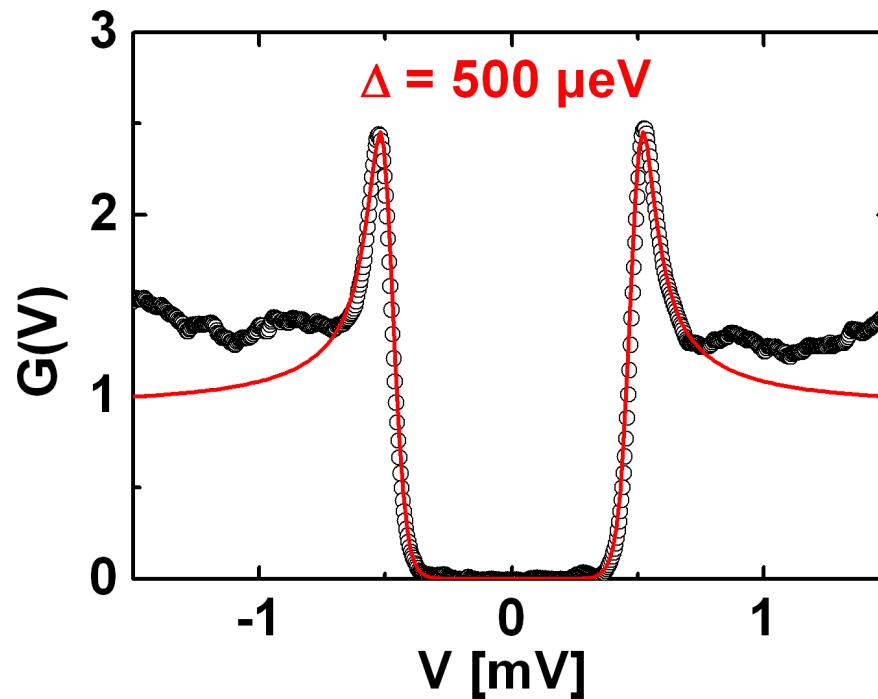


D. Shahar and Z. Ovadyahu, Phys. Rev. B 46, 10917 (1992)

STM and transport measurements



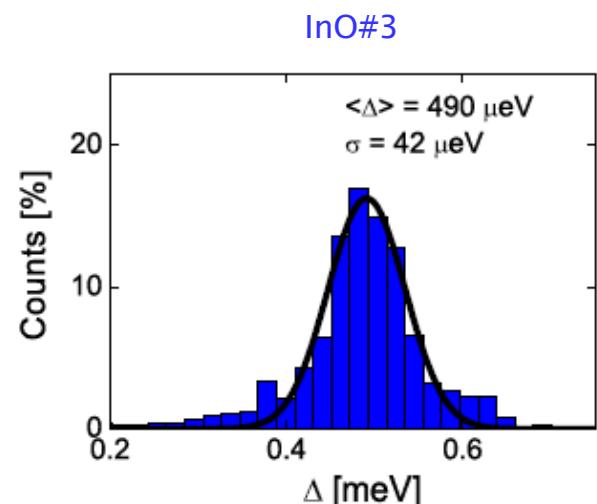
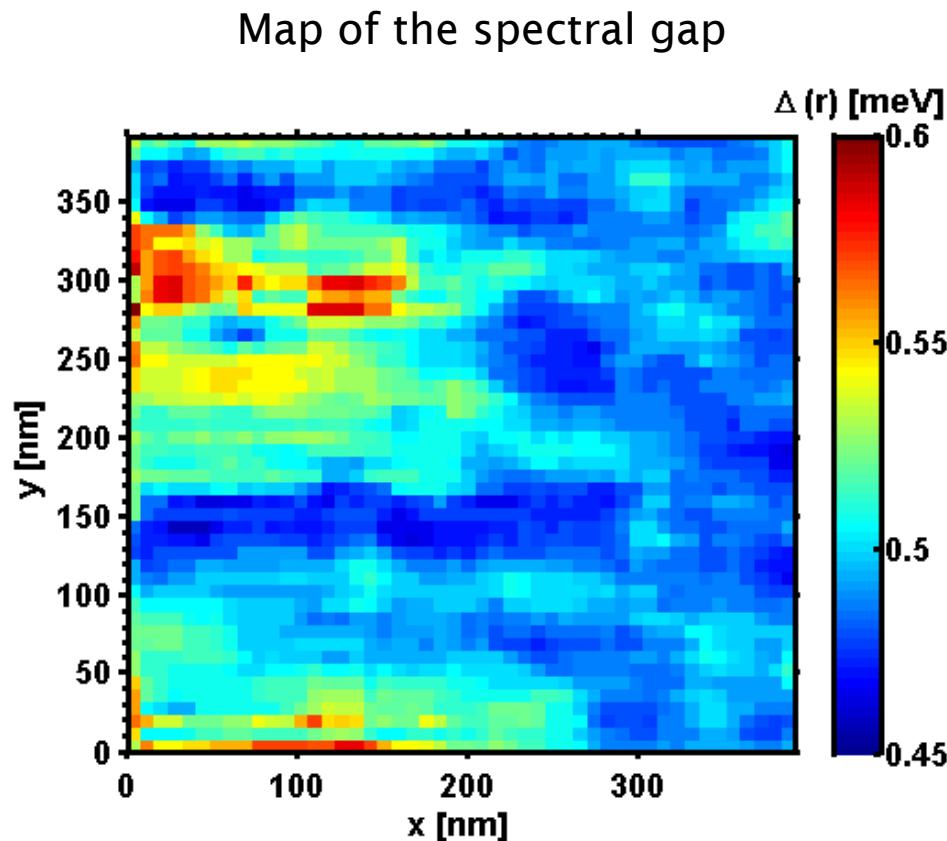
Typical spectrum measured at 50 mK



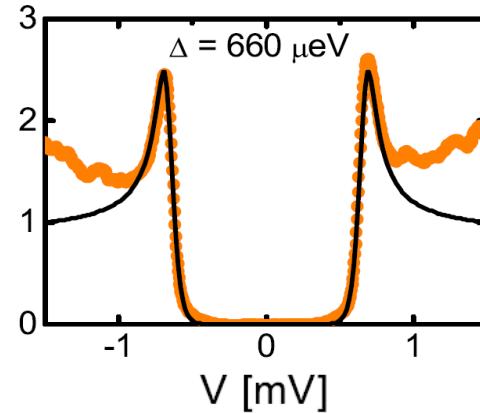
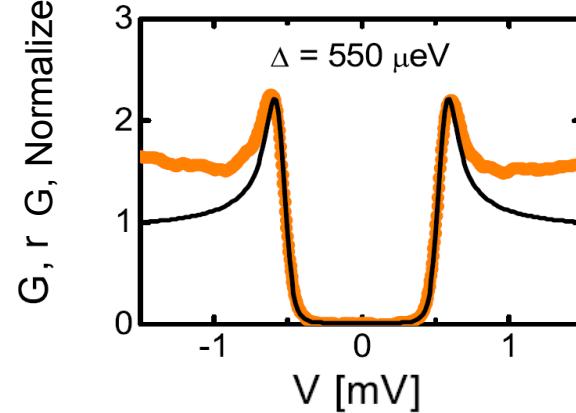
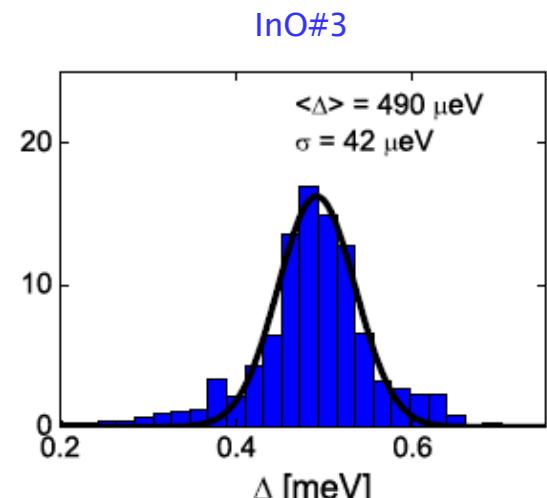
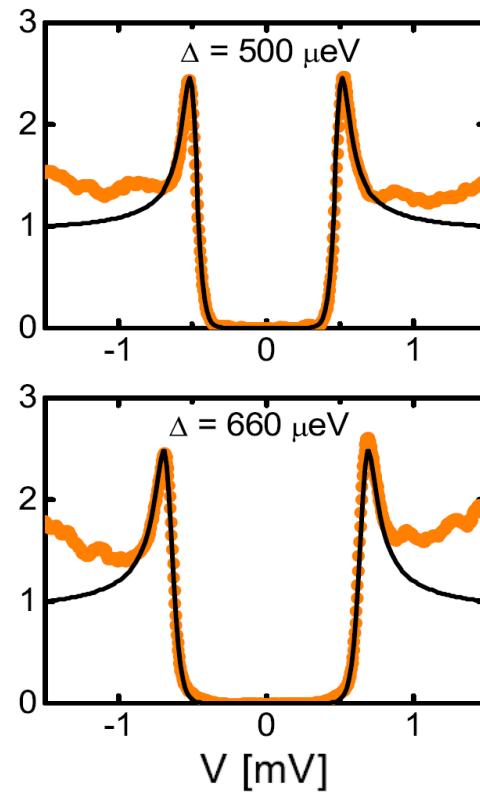
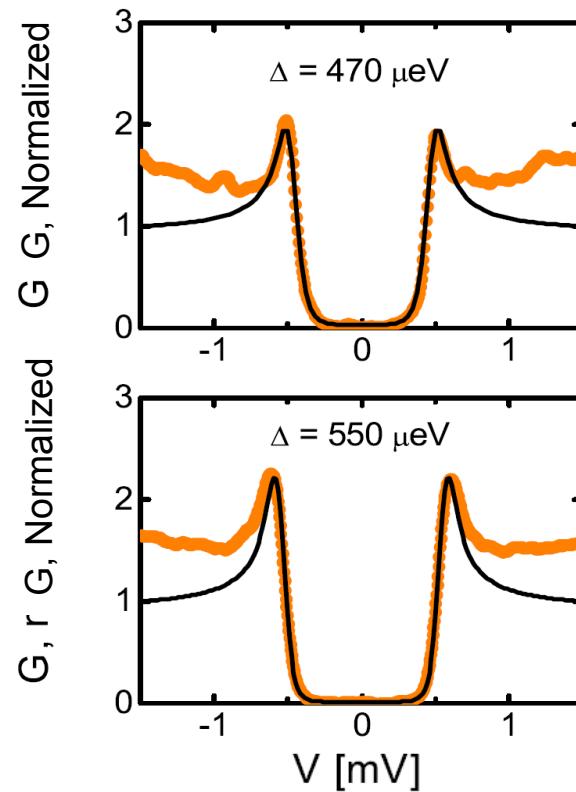
Fit : s-wave BCS density of states

- Absence of quasi-particle excitations at low energies

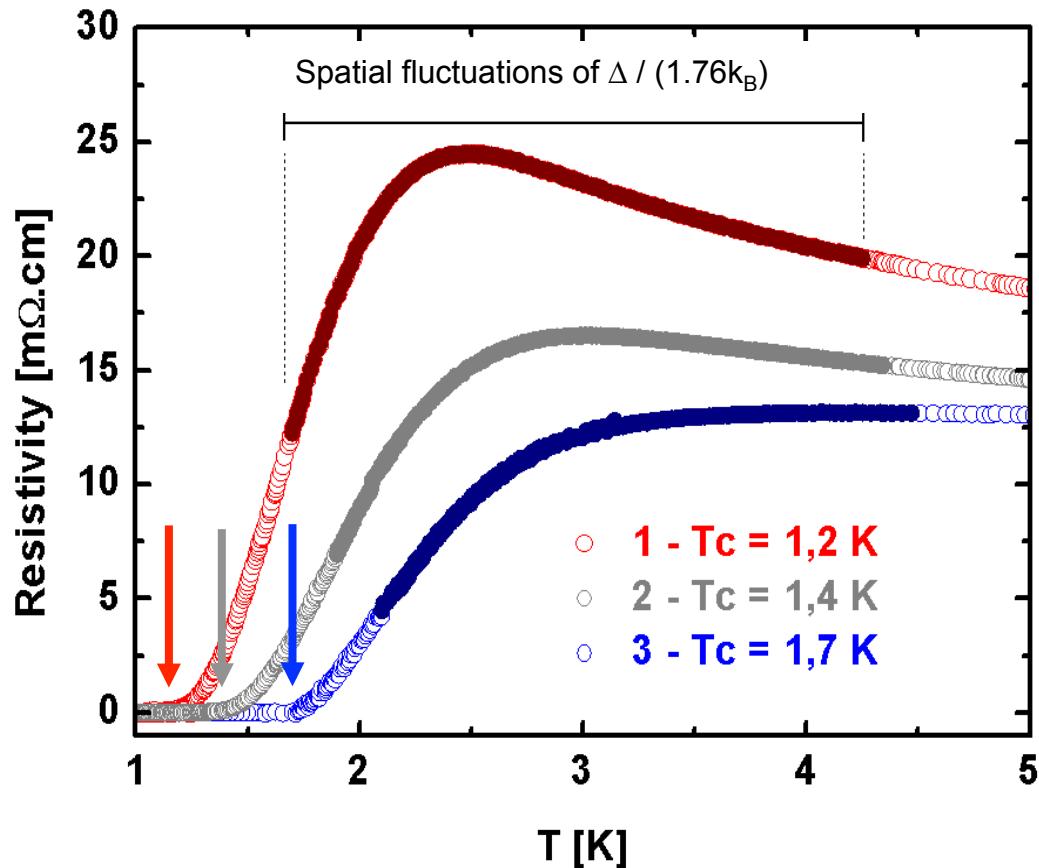
Spatial fluctuations of the spectral gap $\Delta(r)$



Gaussian distribution

Spatial fluctuations of the spectral gap $\Delta(r)$ Spectra measured at different locations ($T=50\text{mK}$)

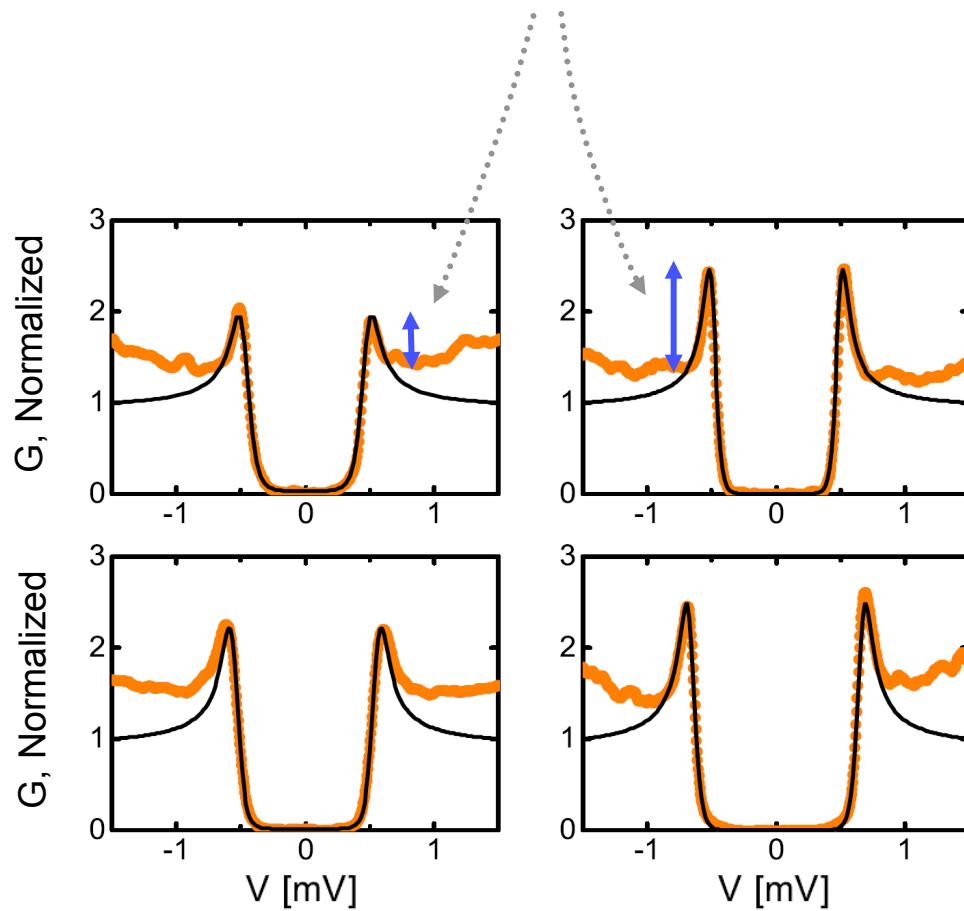
Gaussian distribution

Fluctuations of $\Delta(r)$ and superconducting transition

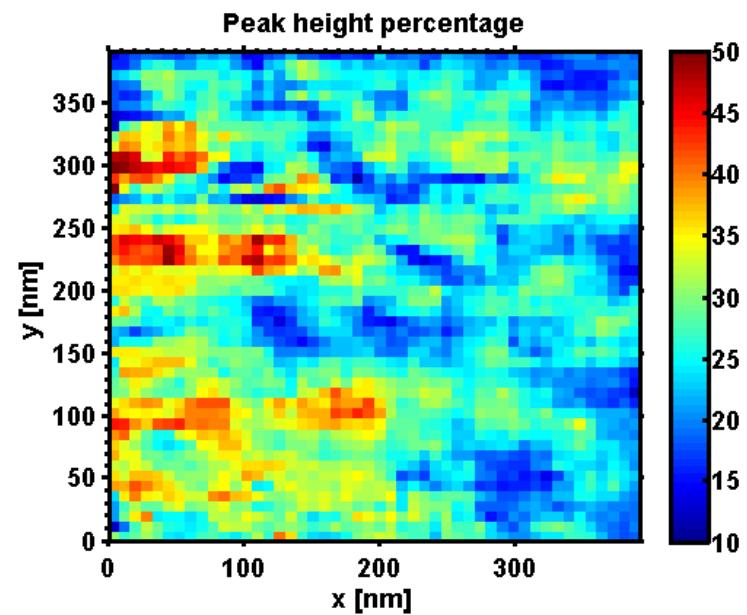
$$3 \leq \frac{\Delta(r)}{k_B T_C} \leq 5.5$$

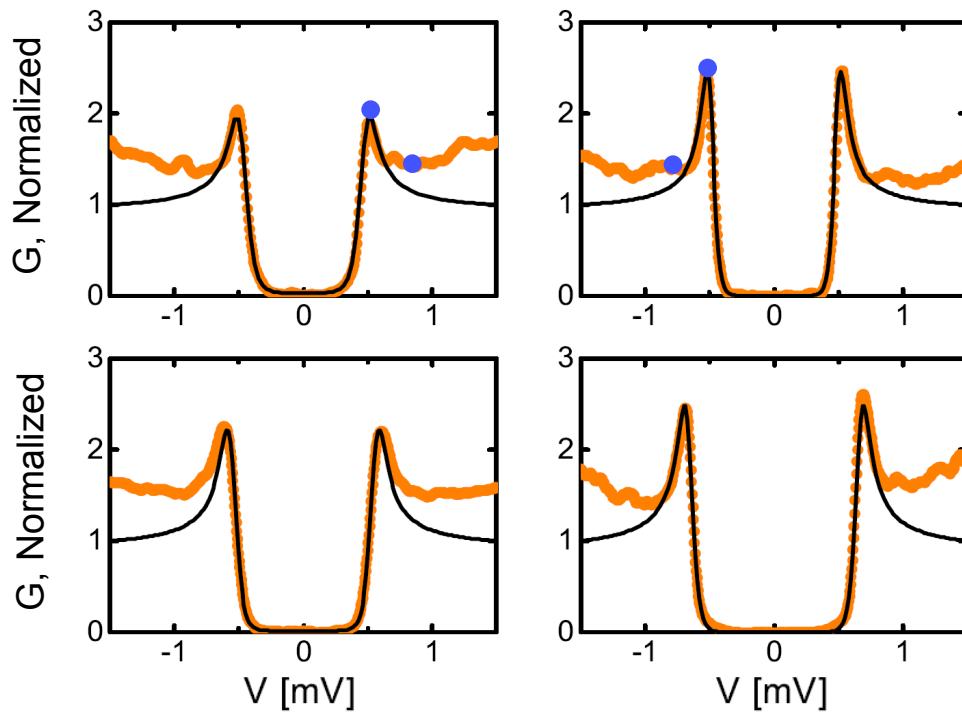
Coherence peaks

Spatial fluctuations of the coherence peaks height



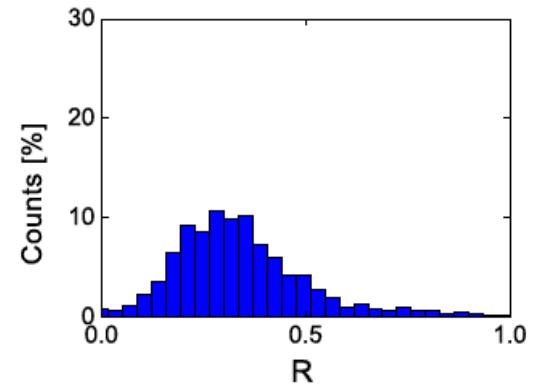
$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$



Spatial fluctuations of the coherence peaks height*Statistical study*

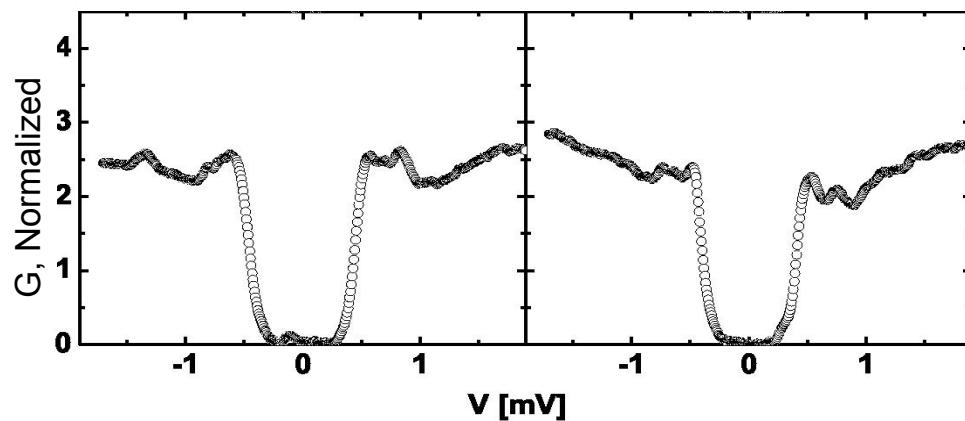
$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$

InO#3



Incoherent spectra

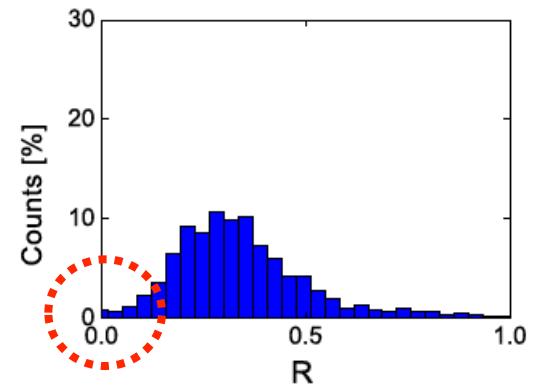
*Full spectral gap
without coherence peaks*



Statistical study

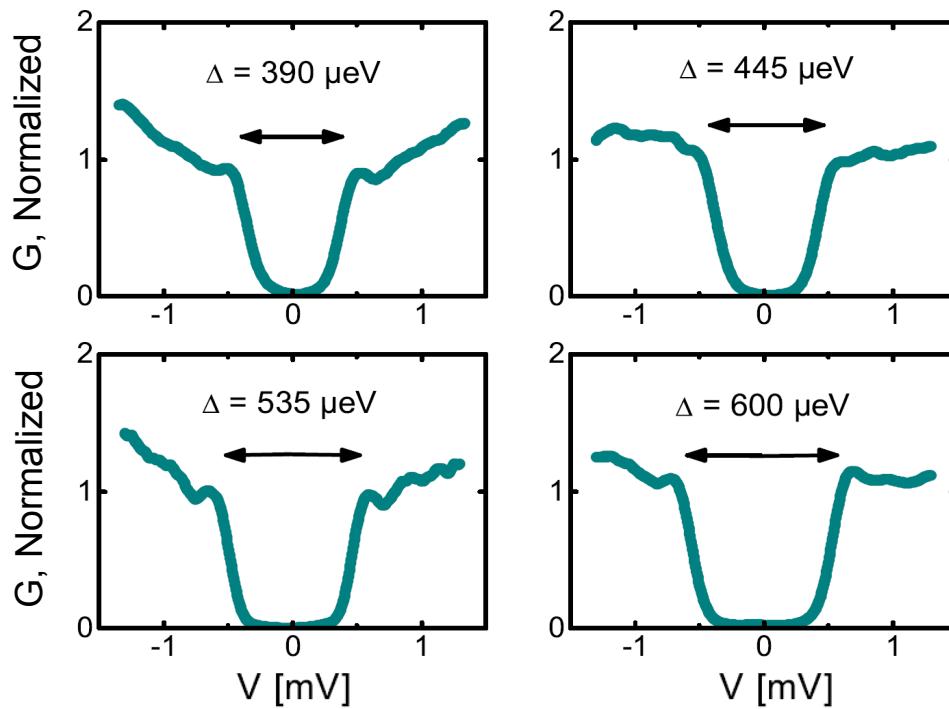
$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$

InO#3



Incoherent spectra

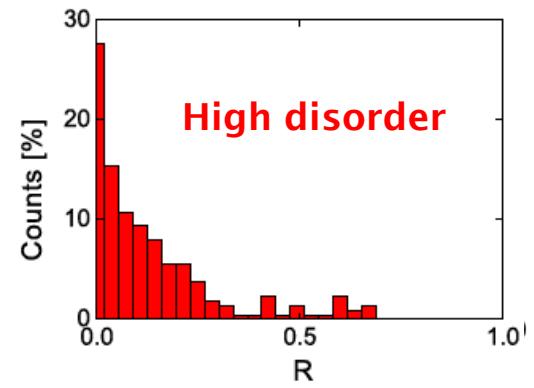
*Full spectral gap
without coherence peaks*



Statistical study

$$R = \frac{G(\Delta) - G(eV > \Delta)}{G(eV > \Delta)}$$

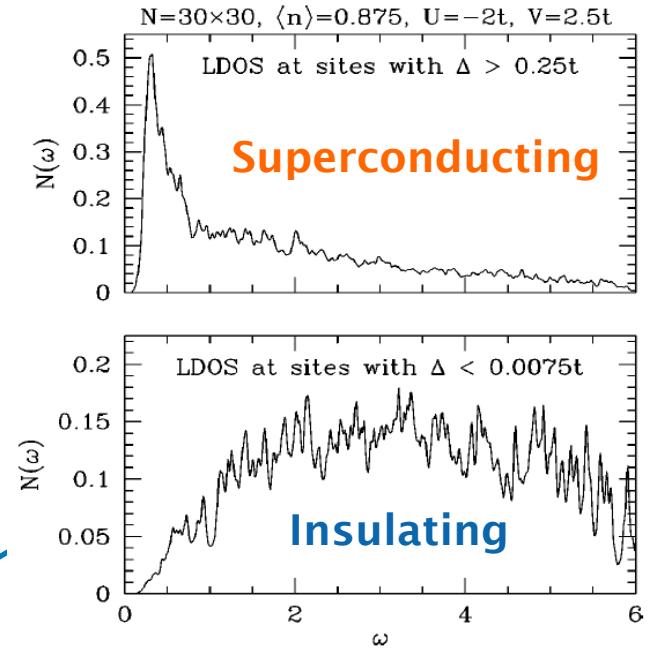
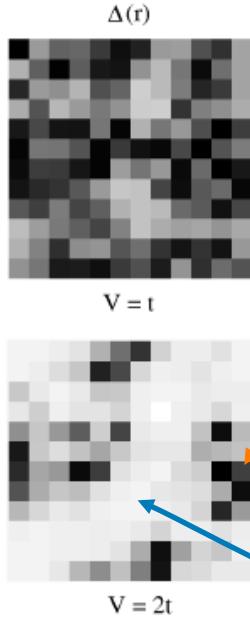
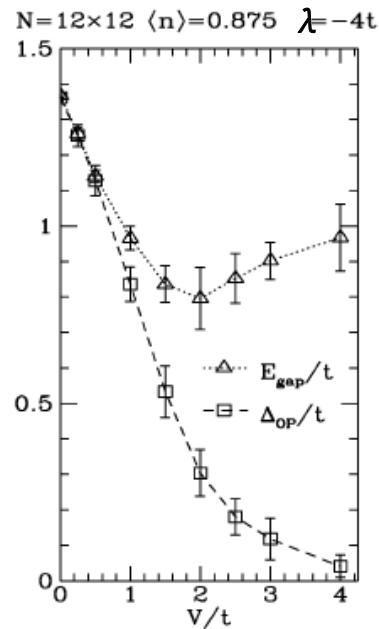
InO#1



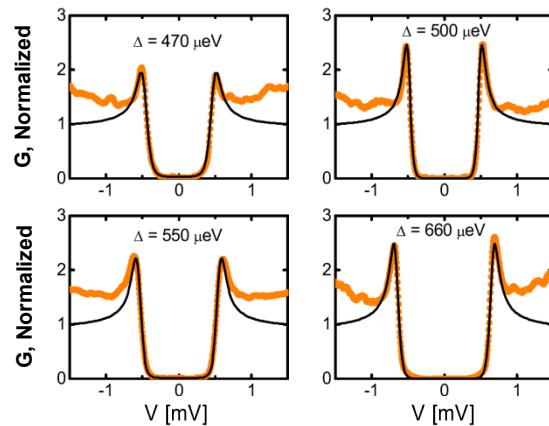
Signature of localized Cooper pairs

A. Ghosal, M. Randeria, N. Trivedi, PRL 81, 3940, (1998) & PRB 65, 014501 (2001)

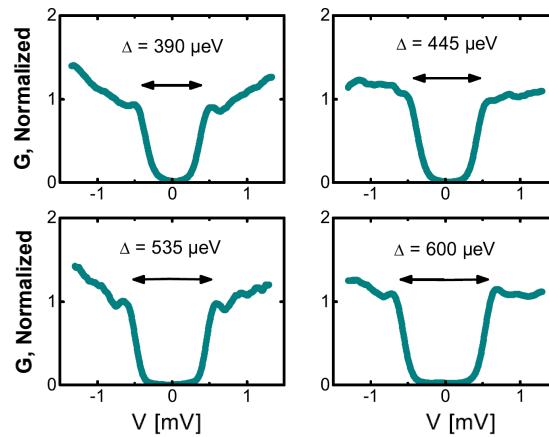
$$H_0 = -t \sum_{\langle i,j \rangle, \sigma} (c_{i\sigma}^+ c_{j\sigma} + h.c.) + \sum_{i,\sigma} (V_i - \mu) n_{i,\sigma} \quad H_{\text{int}} = -\lambda \sum_i n_{i\uparrow} n_{i\downarrow}$$



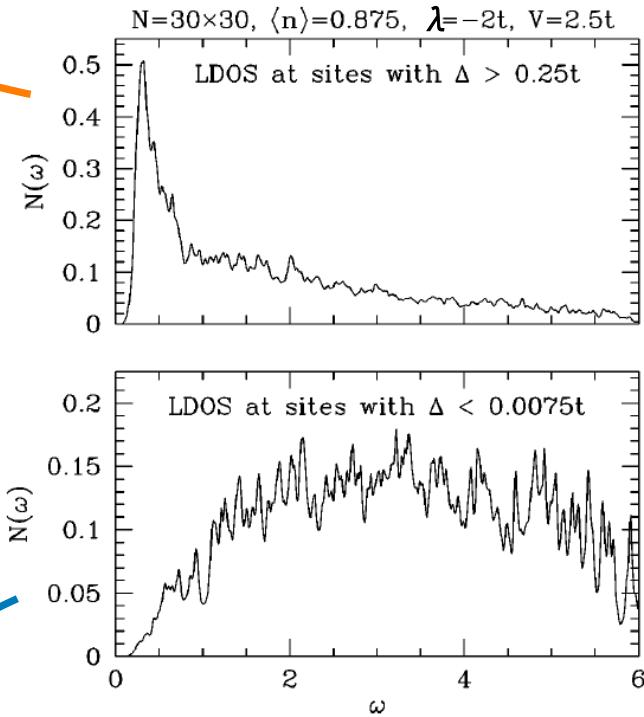
Signature of localized Cooper pairs



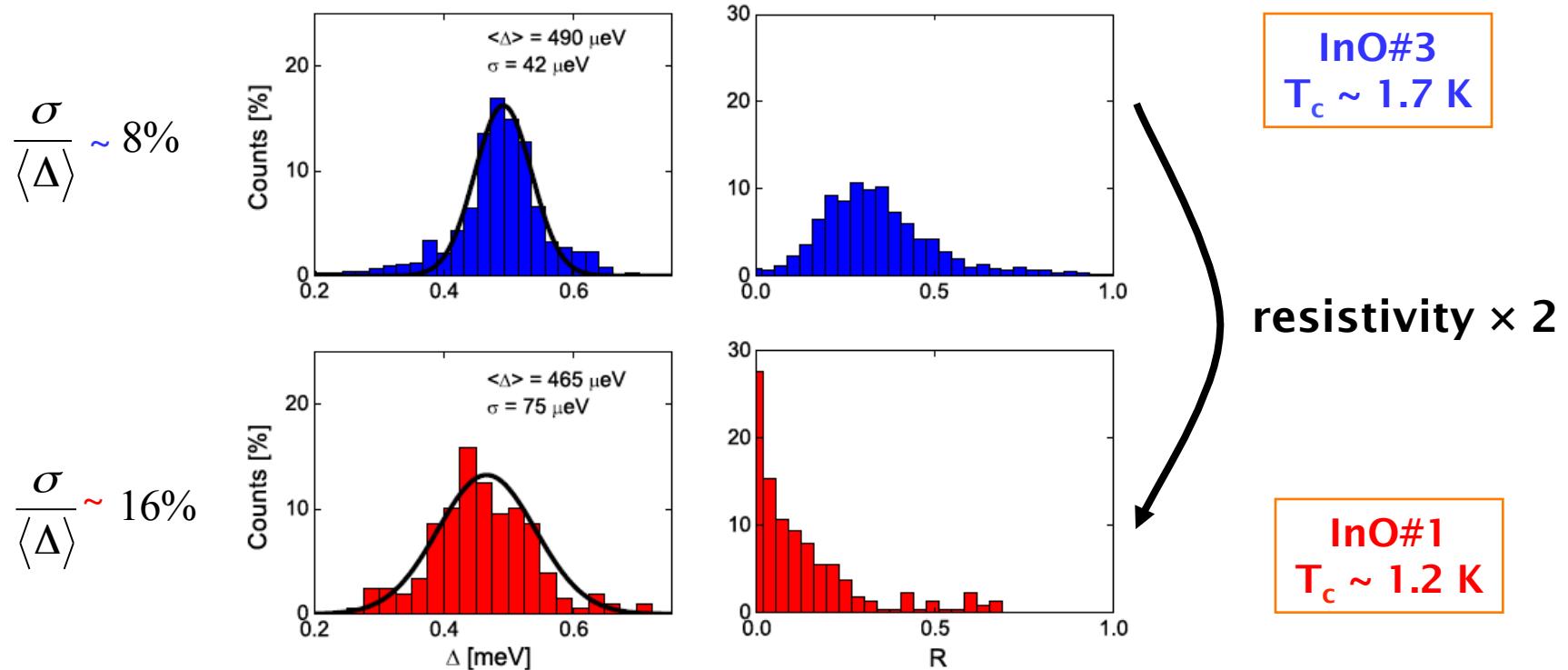
Superconducting gap Δ
⇒ delocalized Cooper pairs



« Insulating » gap E_{gap}
⇒ Localized Cooper pairs



Proliferation of incoherent spectra at the superconductor-insulator transition

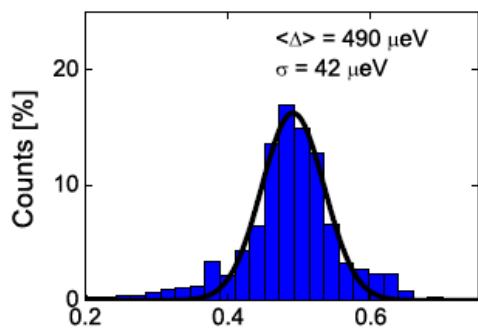


B. Sacépé, et al., *Nature Physics* (2011)

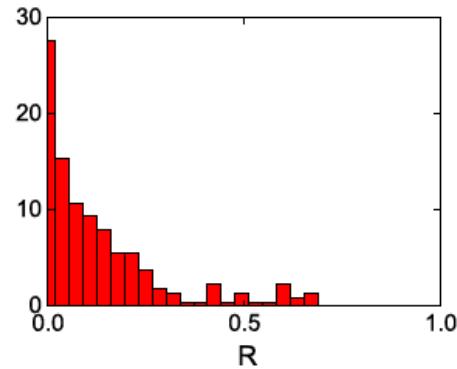
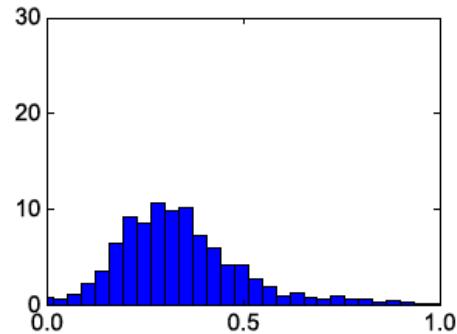
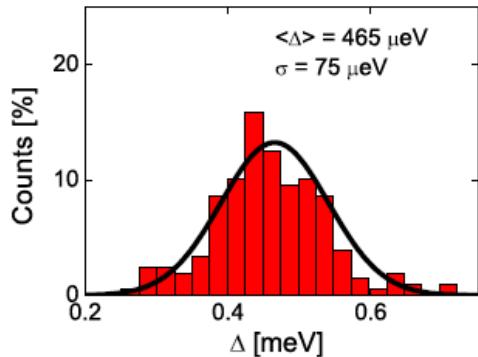
➤ Proliferation of spectra without coherence peaks

Proliferation of incoherent spectra at the superconductor-insulator transition

$$\frac{\sigma}{\langle \Delta \rangle} \sim 8\%$$



$$\frac{\sigma}{\langle \Delta \rangle} \sim 16\%$$



InO#3
 $T_c \sim 1.7 \text{ K}$

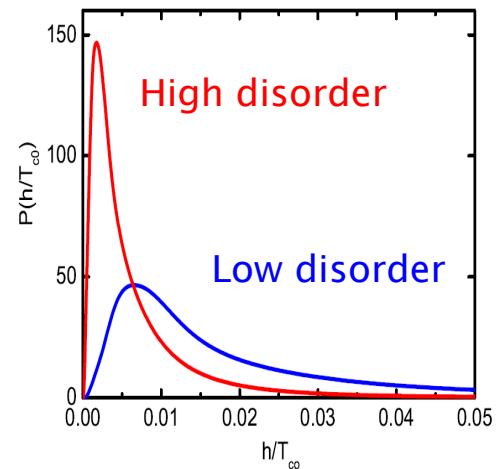
resistivity $\times 2$

InO#1
 $T_c \sim 1.2 \text{ K}$

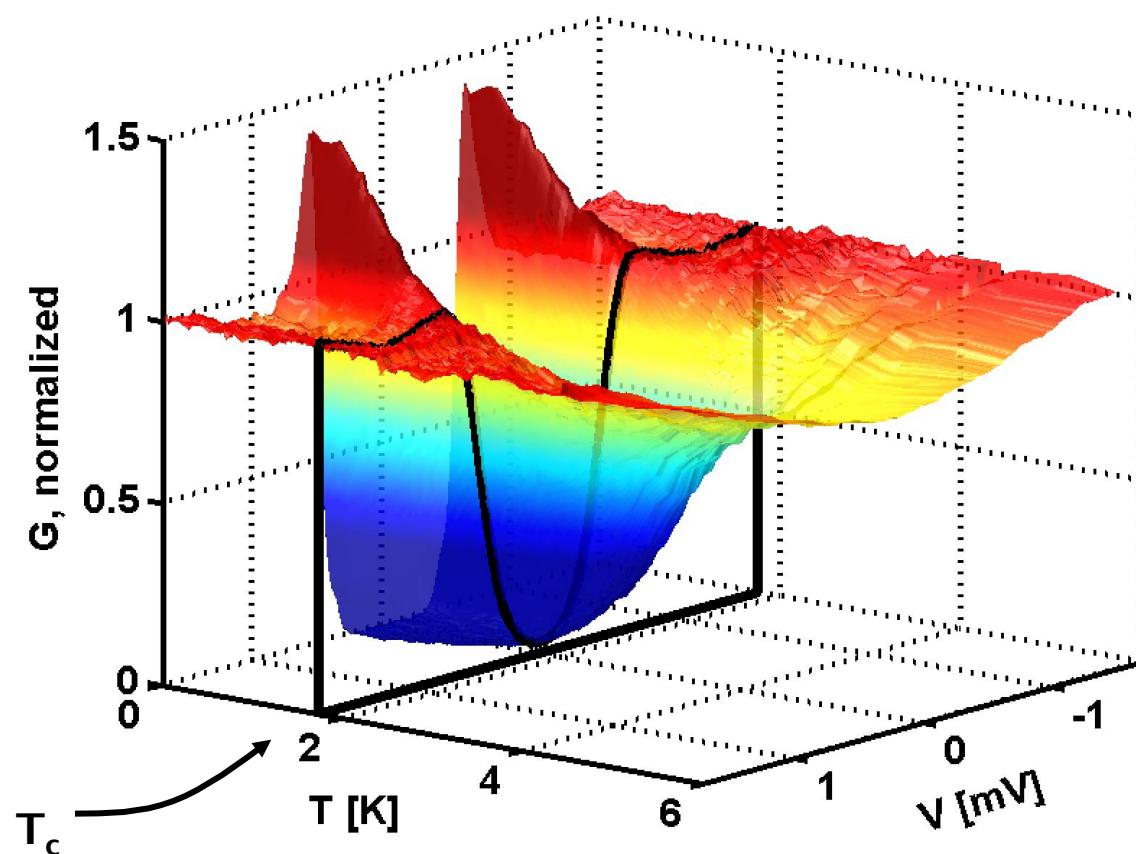
B. Sacépé, et al., *Nature Physics* (2011)

➤ Proliferation of spectra without coherence peaks

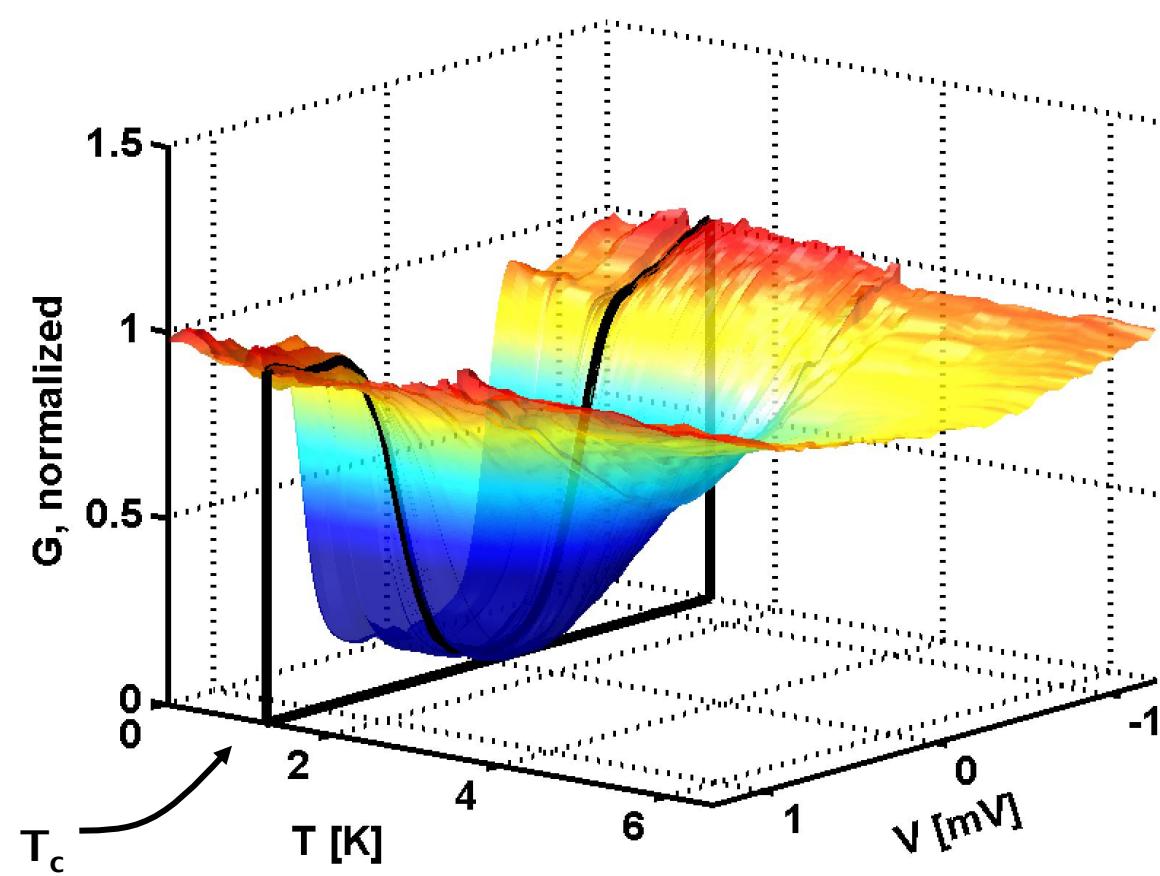
M. Feigel'man et al., *Phys. Rev. Lett.* **98**, 027001 (2007) ; *Ann.Phys.* **325**, 1390 (2010)



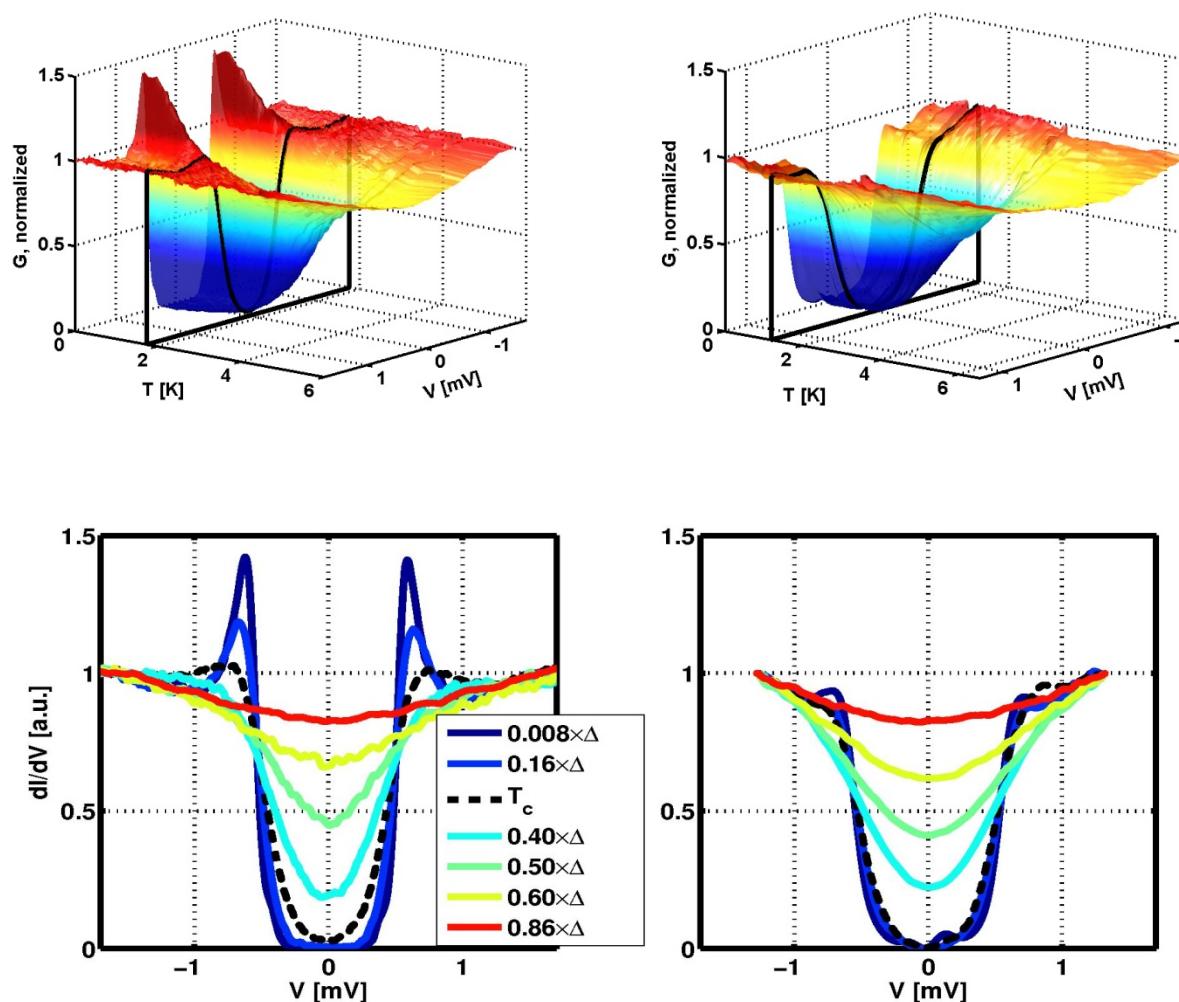
Pseudogap state above T_c



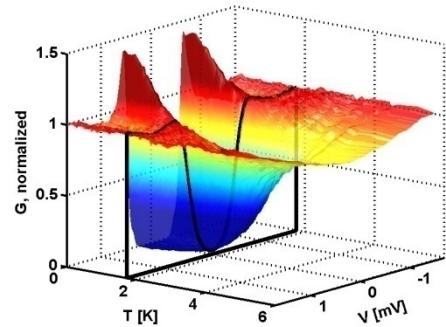
Pseudogap state above T_c



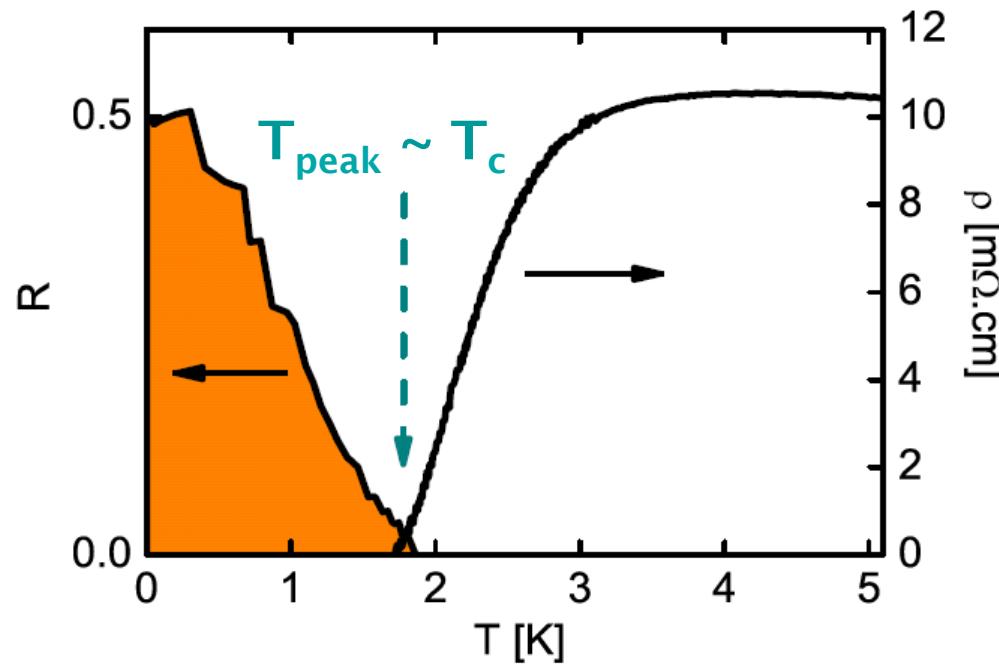
Pseudogap state above Tc



Definition of T_c

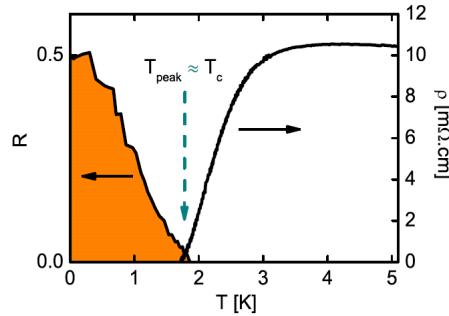


*Macroscopic quantum phase coherence
probed at a local scale*

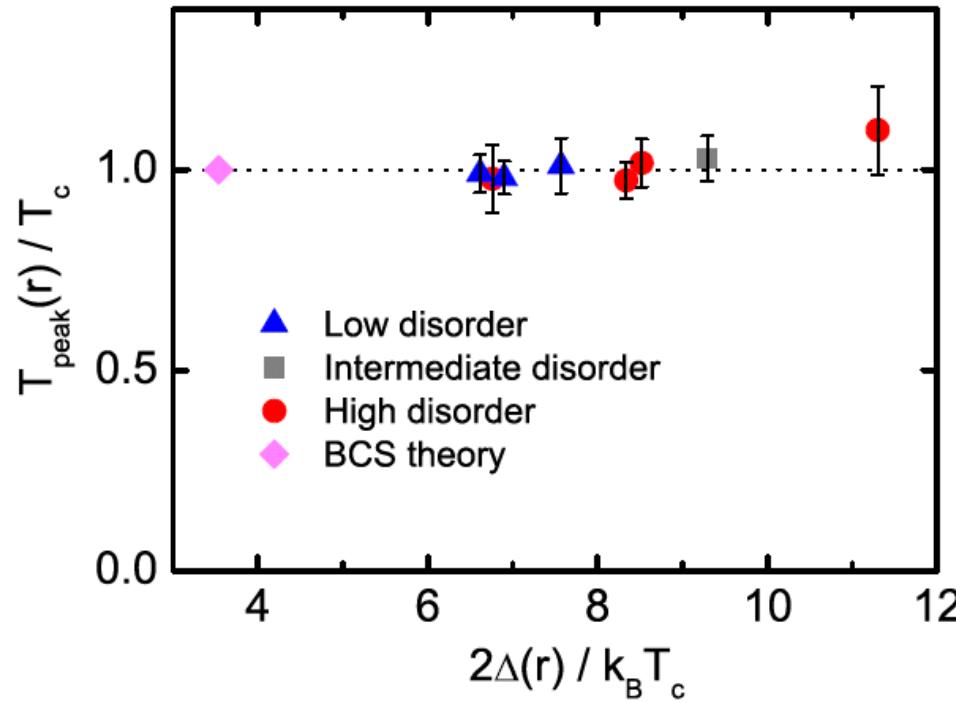


- BCS peaks appear along with superconducting phase coherence

Definition of T_c



*Macroscopic quantum phase coherence
probed at a local scale*



- Phase coherence signaled at T_c independently of $\Delta(r)$
- Justification of T_c

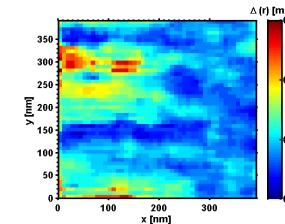
Signatures of the localization of Cooper pairs

A. Ghosal, M. Randeria, N. Trivedi, *PRL* **81**, 3940, (1998) & *PRB* **65**, 014501 (2001)

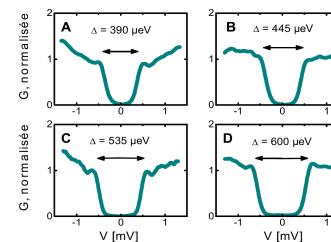
K. Bouadim, Y. L. Loh, M. Randeria, N. Trivedi, *Nature Physics* (2011)

M. Feigel'man et al., *Phys. Rev. Lett.* **98**, 027001 (2007) ; *Ann.Phys.* **325**, 1390 (2010)

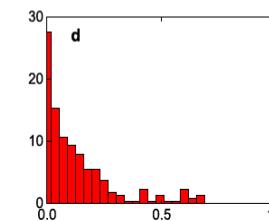
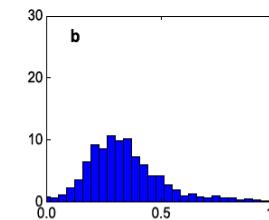
- Spatial fluctuations of the spectral gap



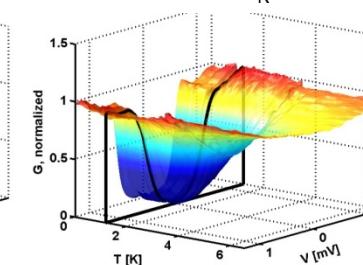
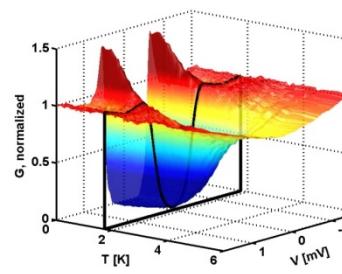
- rectangular-shaped" gap at $T \ll T_c$



- Statistic distribution of coherence peaks height



- Pseudogap regime above T_c



- Anomalously large spectral gap $6 \leq \frac{2E_{gap}(r)}{k_B T_C} \leq 11$

Superconductivity beyond the mobility edge

M. Feigel'man *et al.*, *Phys. Rev. Lett.* **98**, 027001, (2007)

M. Feigel'man *et al.*, *Ann. Phys.* **325**, 1390 (2010)

BCS model built on fractal eigenfunctions of the Anderson problem

- ⇒ $E_{\text{gap}} = \Delta_p + \Delta_{\text{BCS}}$
- Δ_p “parity gap”: pairing of 2 electrons in localized wave functions
 - Δ_{BCS} “BCS gap”: long-range SC order between localized pairs

Two contributions to the spectral gap

Superconductivity beyond the mobility edge

M. Feigel'man *et al.*, Phys. Rev. Lett. 98, 027001, (2007)

M. Feigel'man *et al.*, Ann. Phys. 325, 1390 (2010)

BCS model built on fractal eigenfunctions of the Anderson problem

$$\Rightarrow E_{\text{gap}} = \Delta_p + \Delta_{\text{BCS}}$$

- Δ_p “parity gap”: pairing of 2 electrons in localized wave functions
- Δ_{BCS} “BCS gap”: long-range SC order between localized pairs

How to measure the SC order parameter ?

- Tunneling spectroscopy
(single-particle DOS)

Tunnel barrier

$$E_{\text{gap}} = \Delta_p + \Delta_{\text{BCS}}$$

“parity gap”  “BCS gap” 

- Point-contact spectroscopy
(Andreev reflection = transfer of pairs)

Transparent interface

$$E_{\text{gap}} = \cancel{\Delta_p} + \Delta_{\text{BCS}}$$

“BCS gap” 

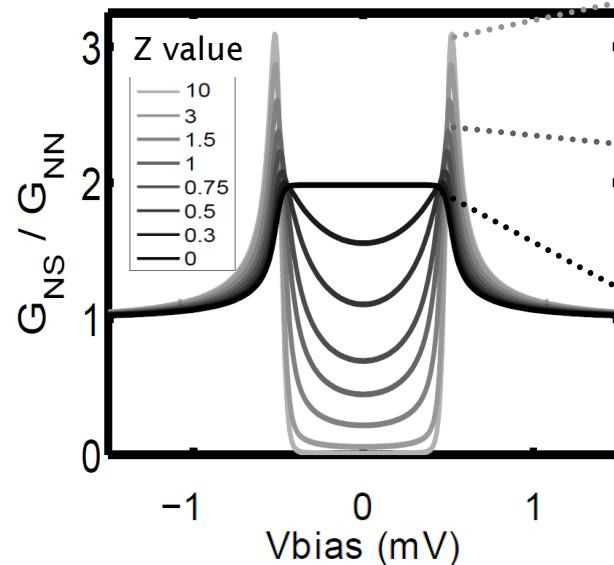
Conductance of a N/S contact

Blonder, G. E., Tinkham, M., and Klapwijk T.M. *Phys. Rev. B* 25, 7 4515 (1982)

Barrier : parameter Z



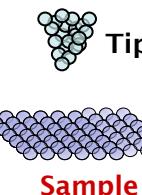
Transmission : $T = 1 / (1 + Z^2)$



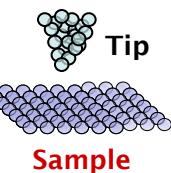
- Single-particle transfer $\sim T$
- Two-particles transfer $\sim T^2$

Tunnel regime

$$Z \gg 1$$

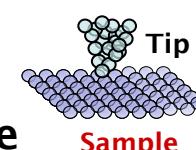


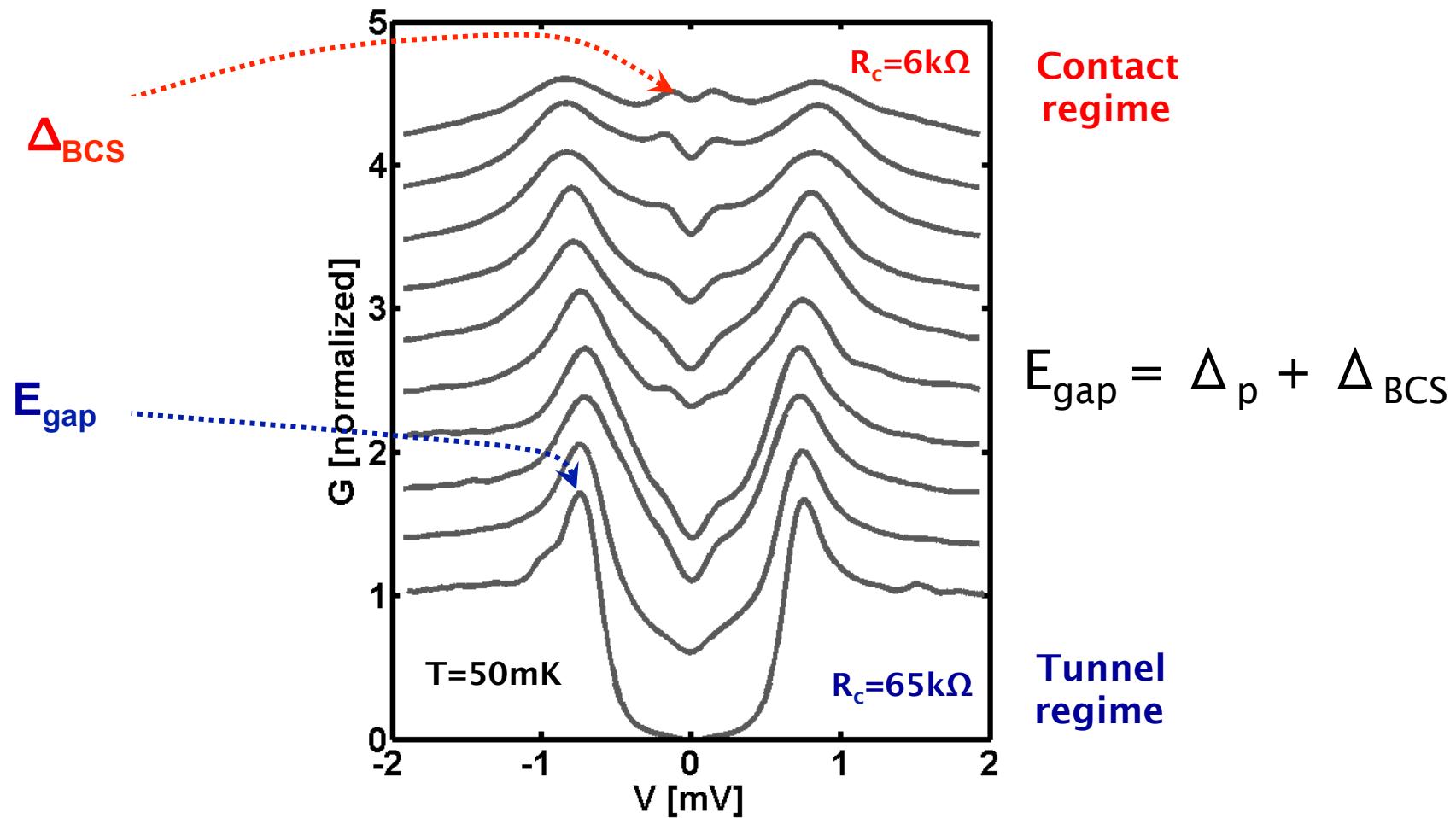
$$Z \sim 1$$

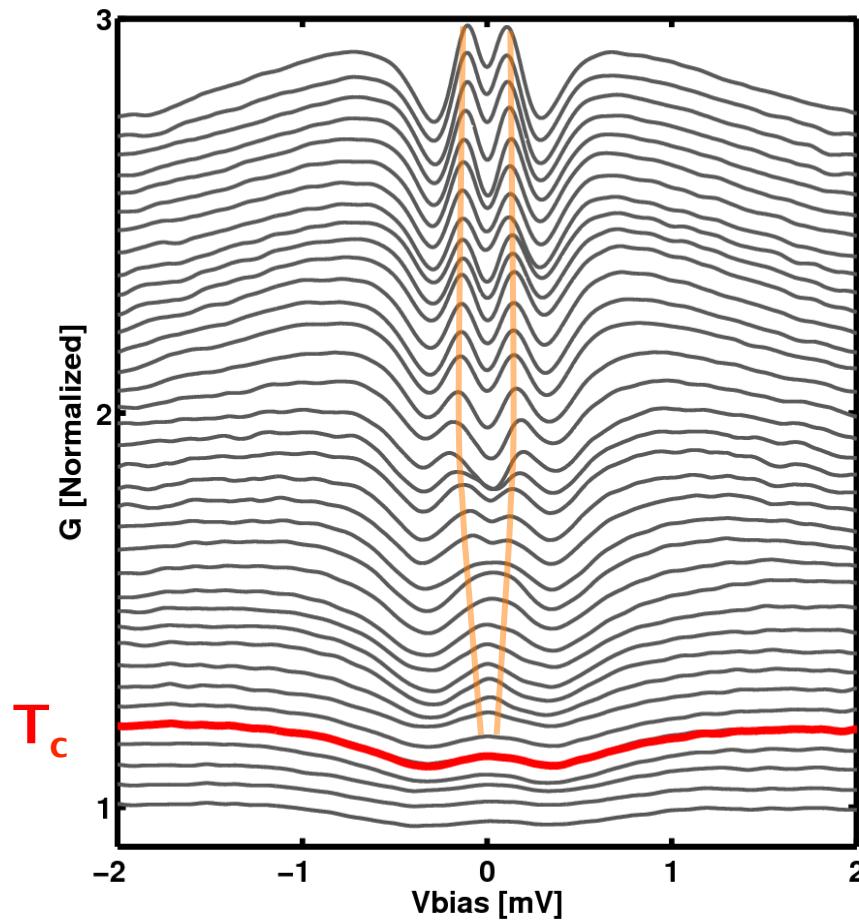


Contact regime

$$Z \ll 1$$



From tunnel to contact in a-InOx

T-evolution of Andreev signal

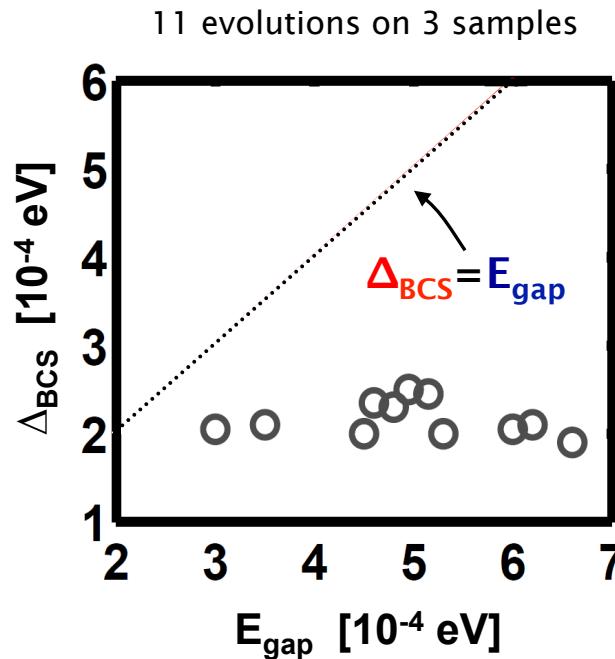
$$E_{\text{gap}}(T) = \Delta_p + \Delta_{\text{BCS}}(T)$$

- . Δ_{BCS} evolves between 0 and $\sim T_c$
- . E_{gap} evolves between 0 and $\sim 3-4 T_c$

- E_{gap} and Δ_{BCS} evolve on distinct temperature range
- Δ_{BCS} : local signature of SC phase coherence

Two distinct energy scales in a-InO_x

$$E_{\text{gap}}(\mathbf{r}) = \Delta_p(\mathbf{r}) + \Delta_{\text{BCS}}$$

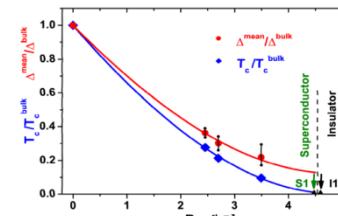


- Δ_{BCS} probed by AR remains uniform
- E_{gap} probed by STS fluctuates

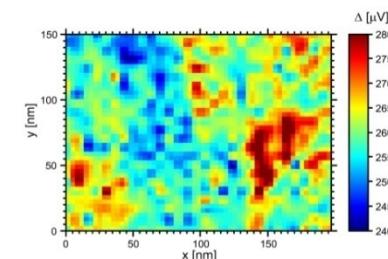
➤ Distinct energy scales for pairing and coherence
in disordered a-InO_x

Conclusion : Fluctuation and localization of preformed Cooper pairs

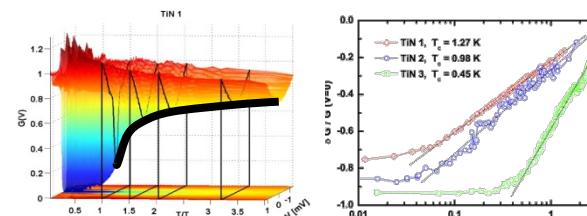
- Homogeneously disordered system with a continuous decrease of T_c



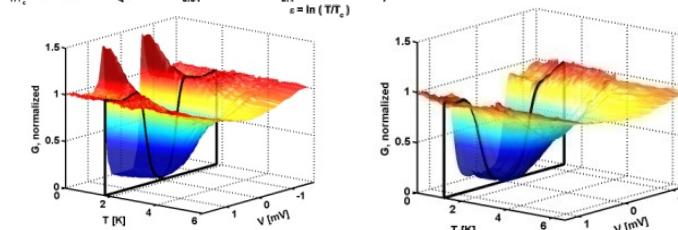
- But inhomogeneous superconducting state at $T < T_c$



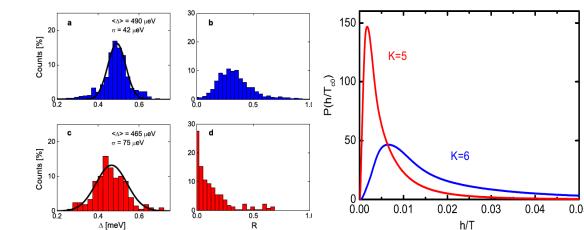
- Fluctuating Cooper-Pairs above T_c



- “Partial” condensation of these preformed pairs below T_c



- SIT occurs through the localization of Cooper-pairs



- Distinct energy scales for pairing and coherence

