

ELECTROSTATIC MODULATION OF THE SUPERFLUID DENSITY OF ULTRATHIN SUPERCONDUCTING $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ FILMS

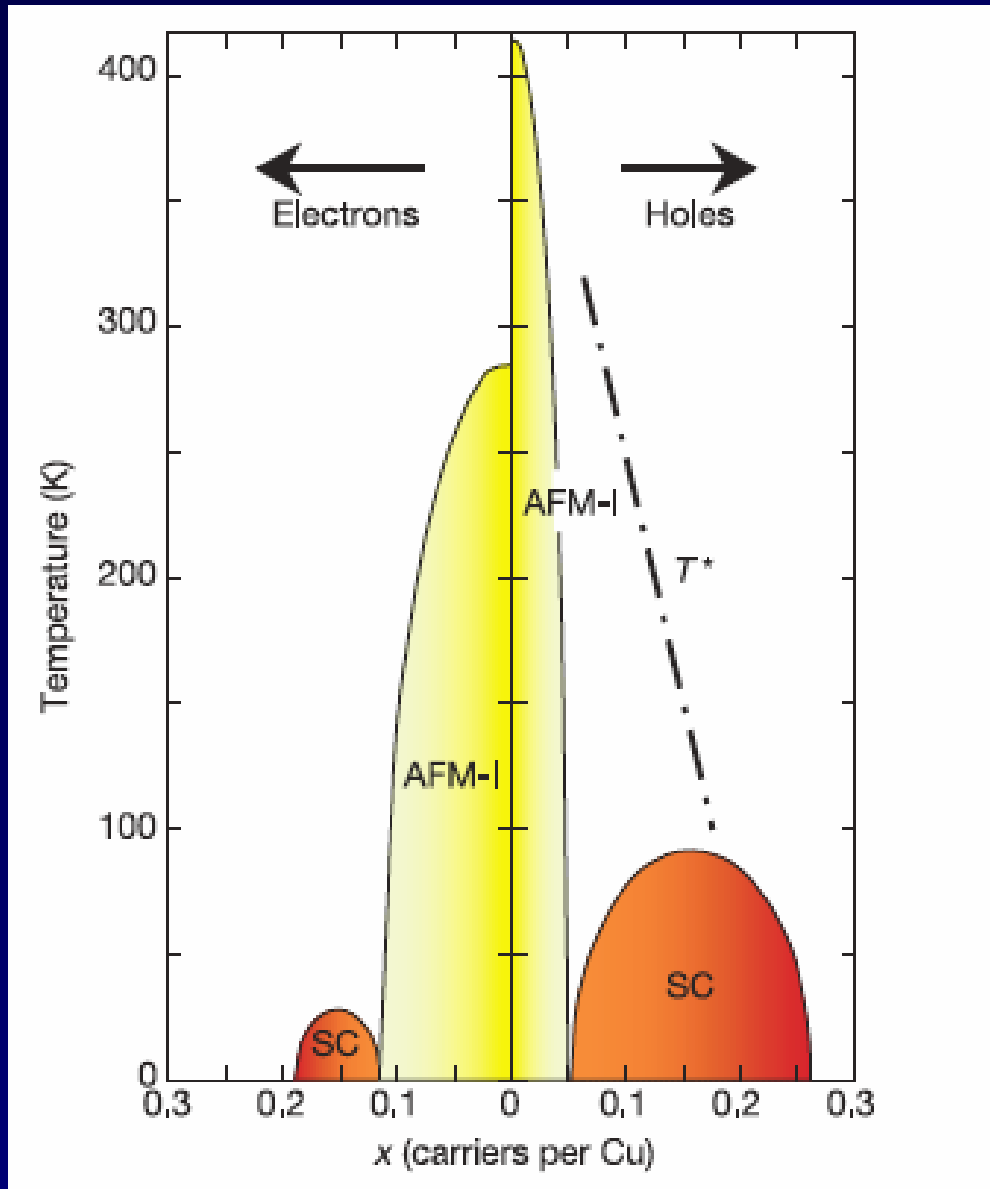
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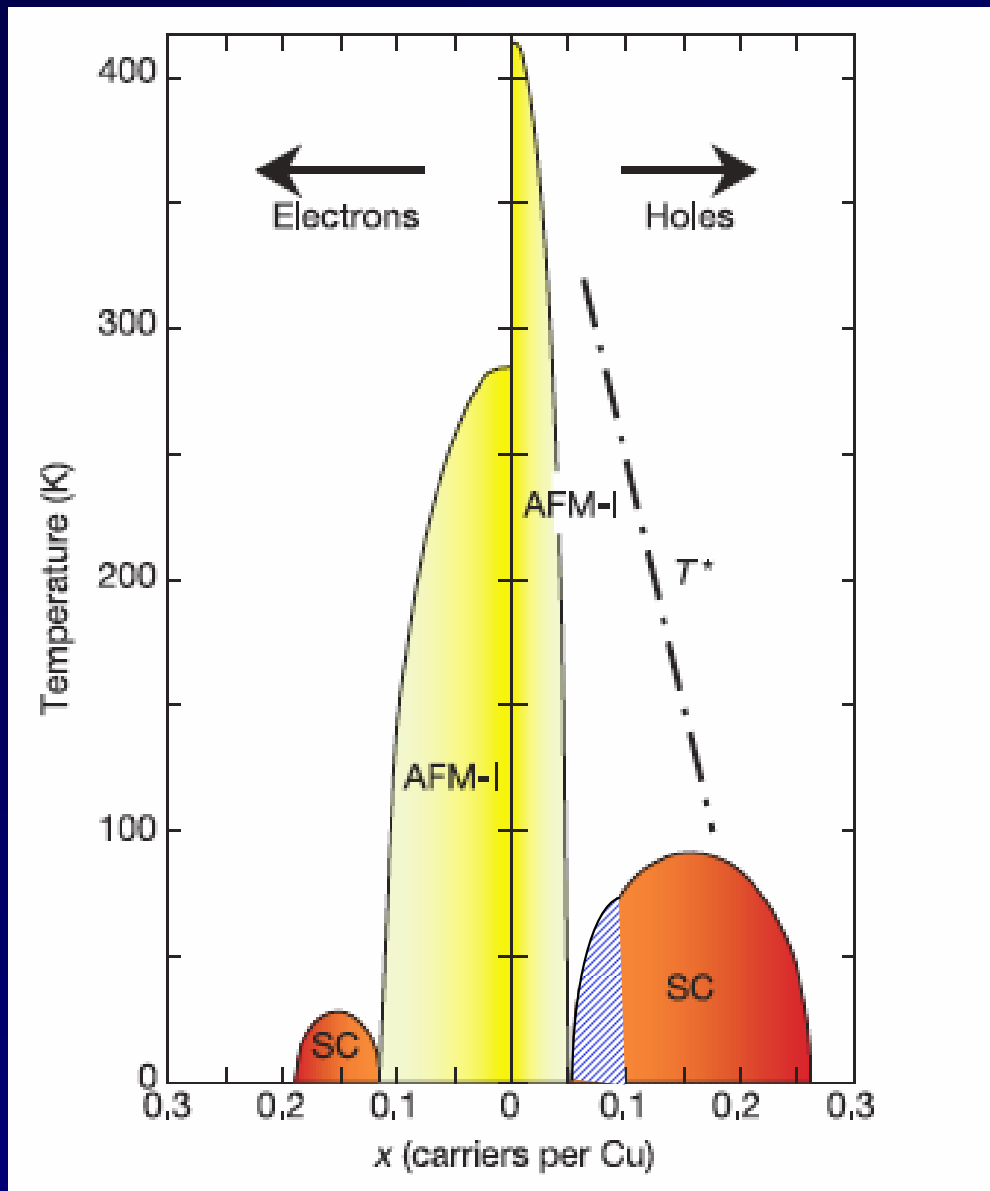


Generic Phase Diagram of High- T_c Superconductors



C.H. Ahn et al., Nature (2003)

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Underdoped regime
(doped Mott insulator) :

$$T_c \propto n_s(T=0)$$

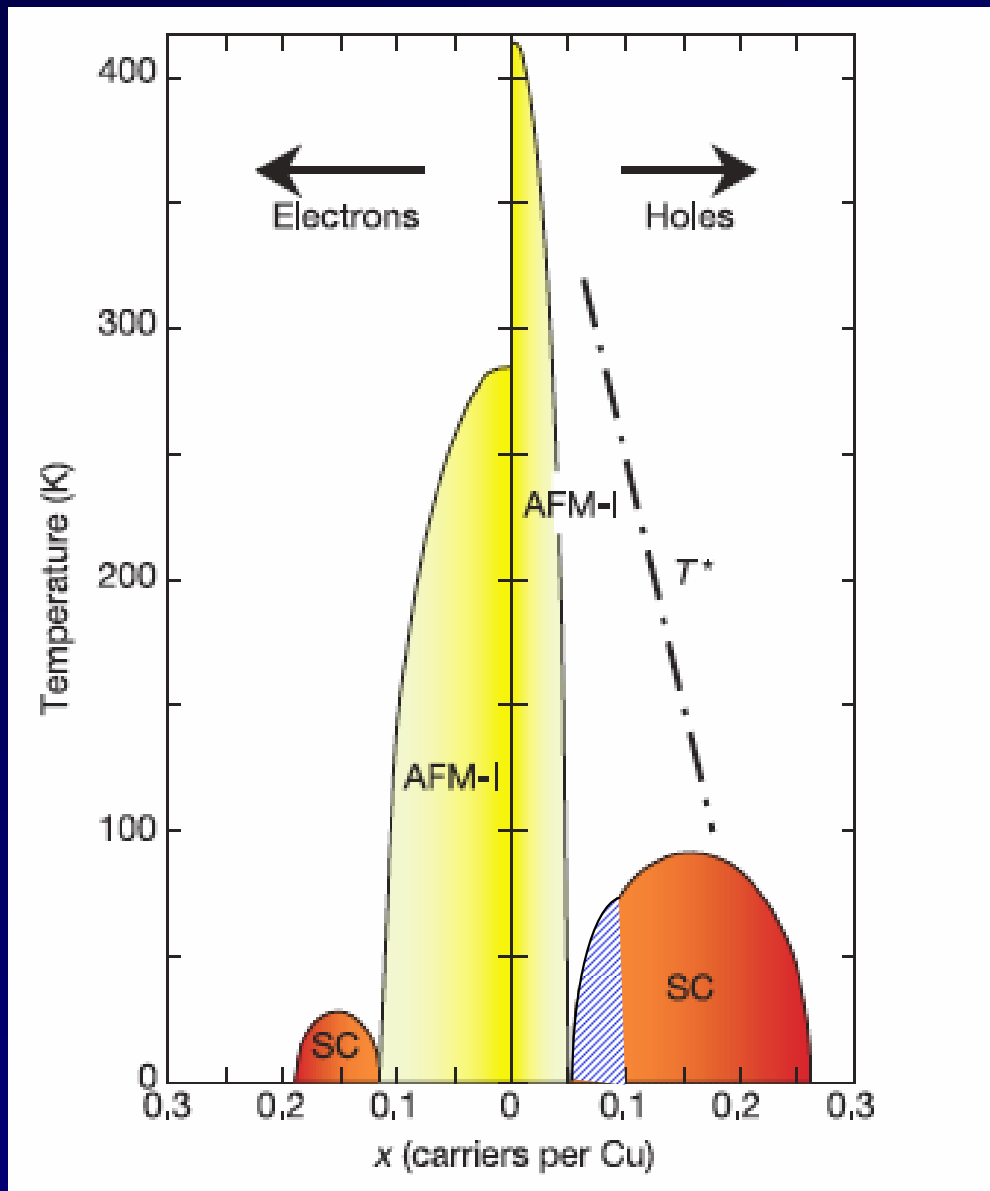
« Uemura relation »
[Y. Uemura *et al.*, PRL (89)]

Changing n_s by « chemical » doping
implies sample-to-sample varying
disorder, thereby complicating the
interpretation of the data



Electrostatic modulation

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C.H. Ahn et al., Nature (2003)

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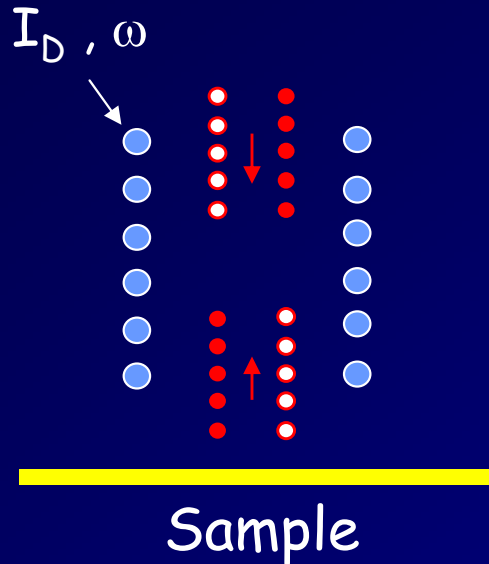
« Uemura relation »
[Y. Uemura *et al.*, PRL (89)]

Connection to experiment
(thin films, thickness d) :

$$L_k^{-1} = e^2 n_s d / m^* \propto \lambda_{ab}^{-2}$$

L_k : kinetic inductance

Complex sheet impedance measurements



Drive (D)-receive (R) two-coil
SQUID-based technique

B. Jeanneret et al., APL (1989)

$\Delta L \sim 1\text{pH}$, $0.1\text{ Hz} < \omega < 10^5\text{ Hz}$

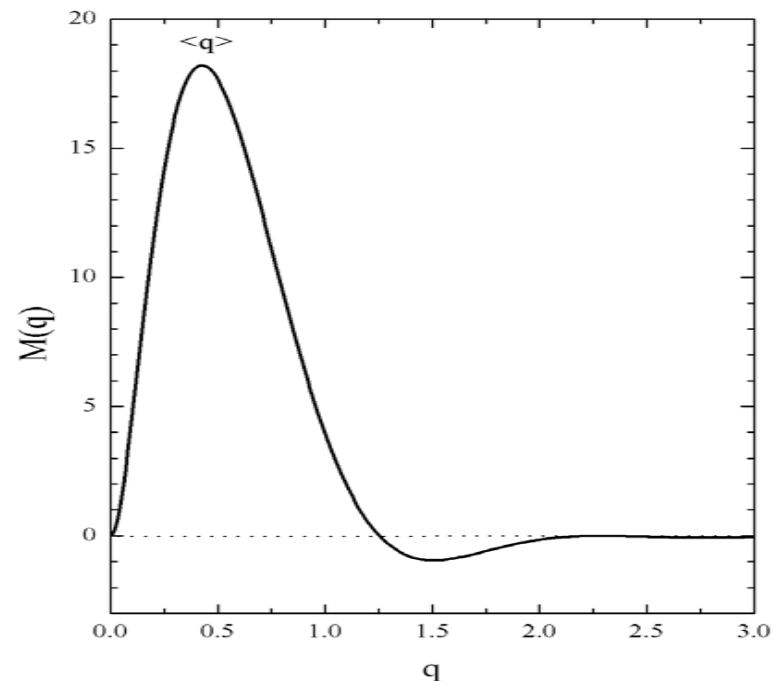
$$\delta M \propto \int_0^{\infty} \{1 + [Z/i\omega m]q\}^{-1} M(q) dq$$

$$Z = R + i\omega L_k$$

$$L_k^{-1} = e^2 n_{s\Box} / m^*$$

$n_{s\Box} = n_s d$: 2D superfluid density

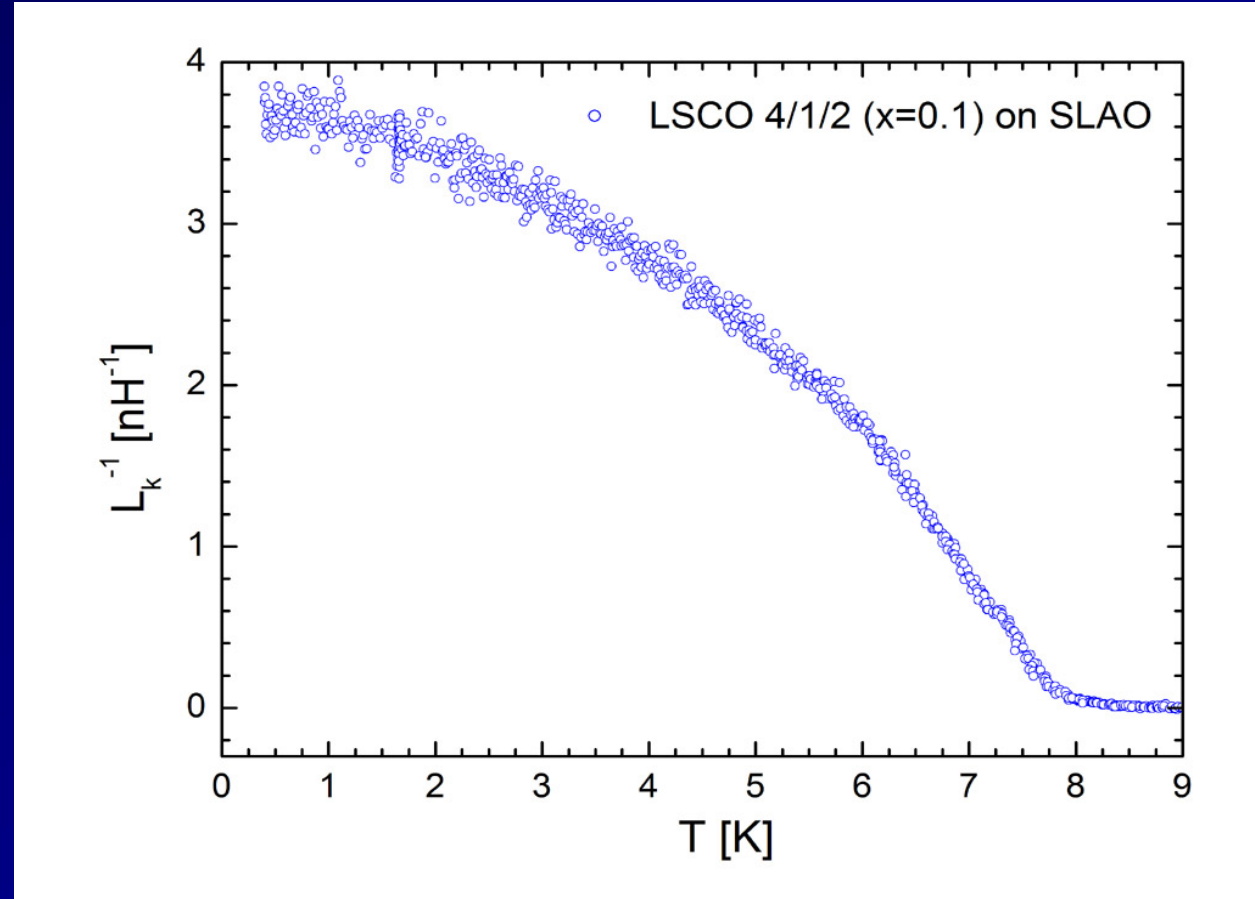
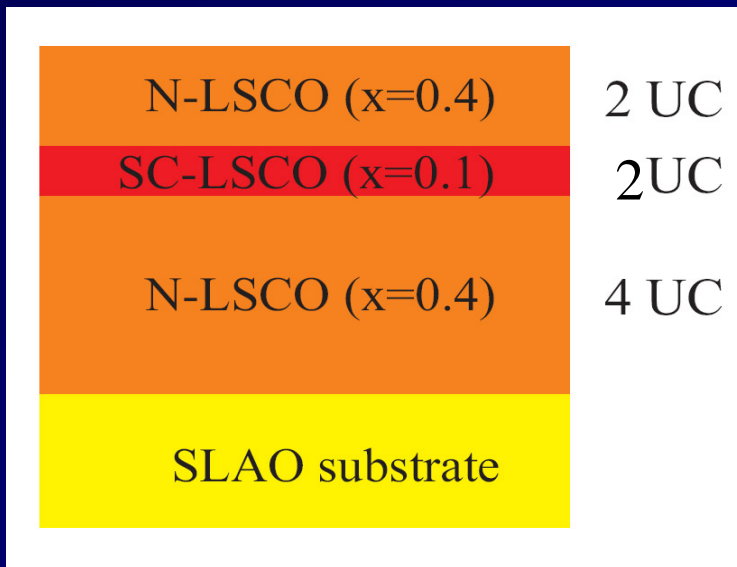
R : dissipation \Rightarrow vortices



Growth of ultrathin LSCO films - Kinetic inductance $L_k^{-1}(T)$

MBE buffer method

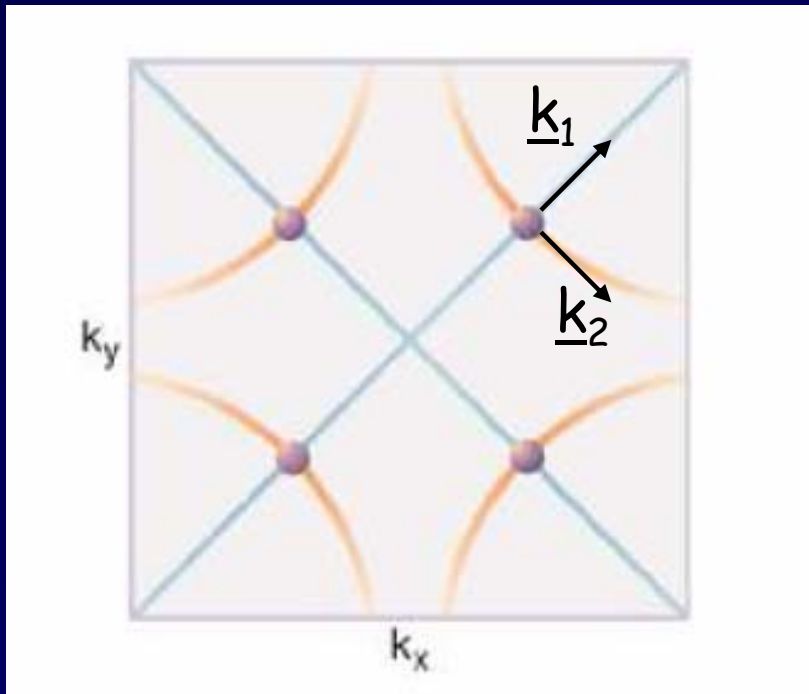
A. Rüfenacht *et al.*, *Solid-State Electronics* 47, 2167 (2003)



J.P. Locquet *et al.*, *Nature* (98)

From $L_k(0) = \mu_0 \lambda_{ab}^2(0)/d$: $\lambda_{ab}(0) = 535 \text{ nm}$

Superconductor with $d_{x^2-y^2}$ pairing symmetry



P.A. Lee, Science (1997)

QP excitation energy :

$$E(\underline{k}) = \hbar[(k_1 v_F)^2 + [(k_2 v_\Delta)^2]^{1/2}]^{1/2}$$

$$v_\Delta = a\Delta_0/\hbar\sqrt{2}$$

QP density of states

[A.C. Durst and P.A. Lee, PRB (2000)]

Pure superconductor :

$$N(\varepsilon) = |\varepsilon|/\pi\hbar^2 v_F v_\Delta$$

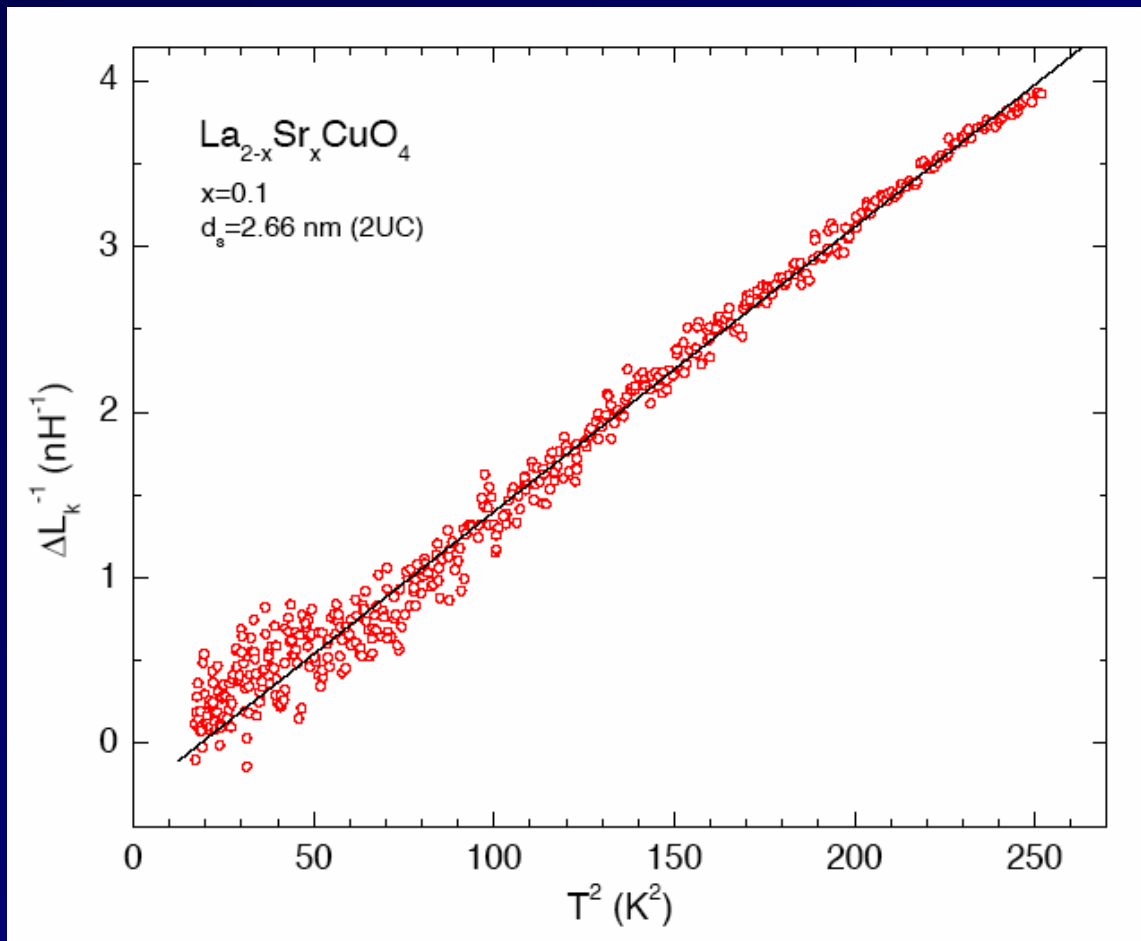
Superconductor with impurities :

$$N(0) = [4(\hbar/\tau)/\pi\hbar^2 v_F v_\Delta] \ln[E_0/(2\pi\hbar/\tau)]$$

τ : QP lifetime , $E_0 = (2E_F\Delta_0)^{1/2}$

Low-temperature ($T \ll T_c$) inverse kinetic inductance change

$$\Delta L_k^{-1} \equiv L_k^{-1}(0) - L_k^{-1}(T)$$



SC with nodal points in the order parameter (*d-wave*) and with impurities :

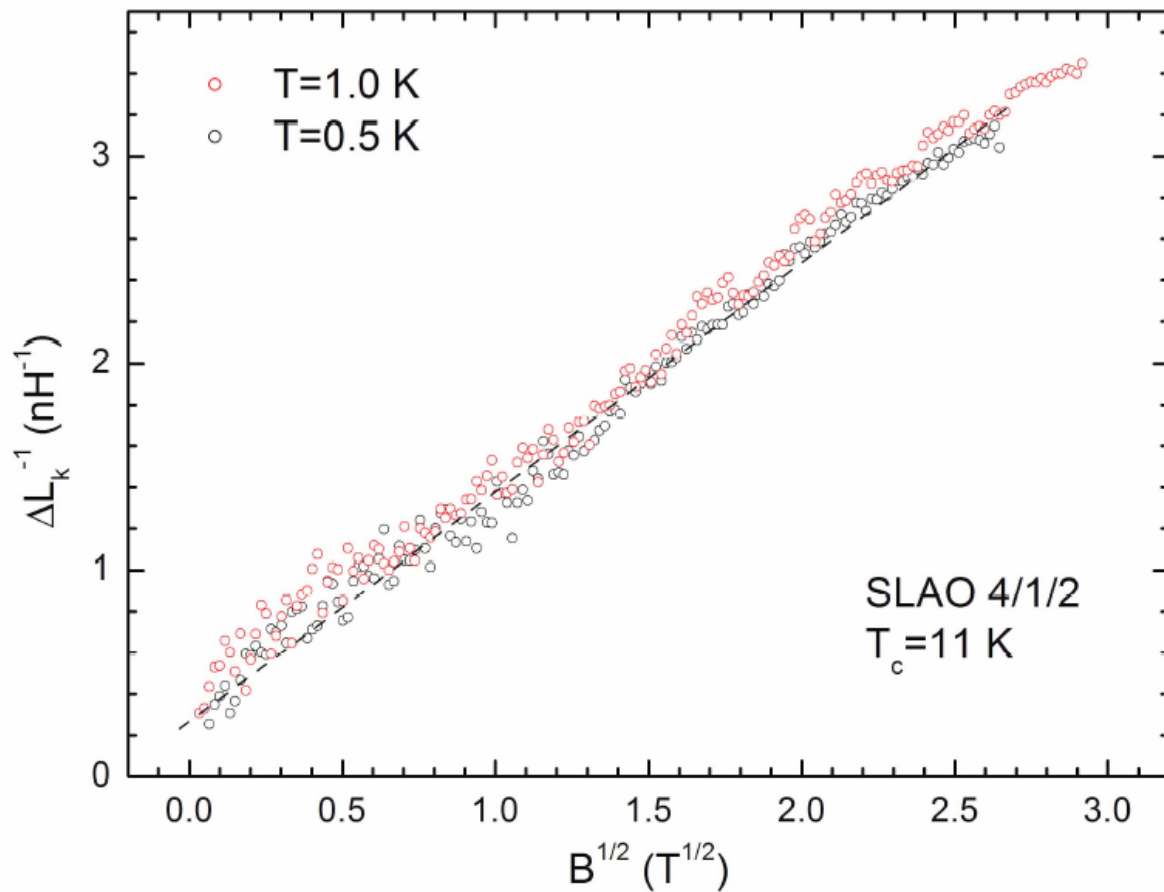
[S.G. Sharapov *et al.*, PRB (2002)]

$$\Delta L_k^{-1}(T) \propto T^2$$

«Pure» SC : $\Delta L_k^{-1}(T) \propto T$

[W.N. Hardy *et al.*, PRL (1993)]

Low-temperature magnetic-field dependence of $\Delta L_k^{-1} \equiv L_k^{-1}(0) - L_k^{-1}(B)$



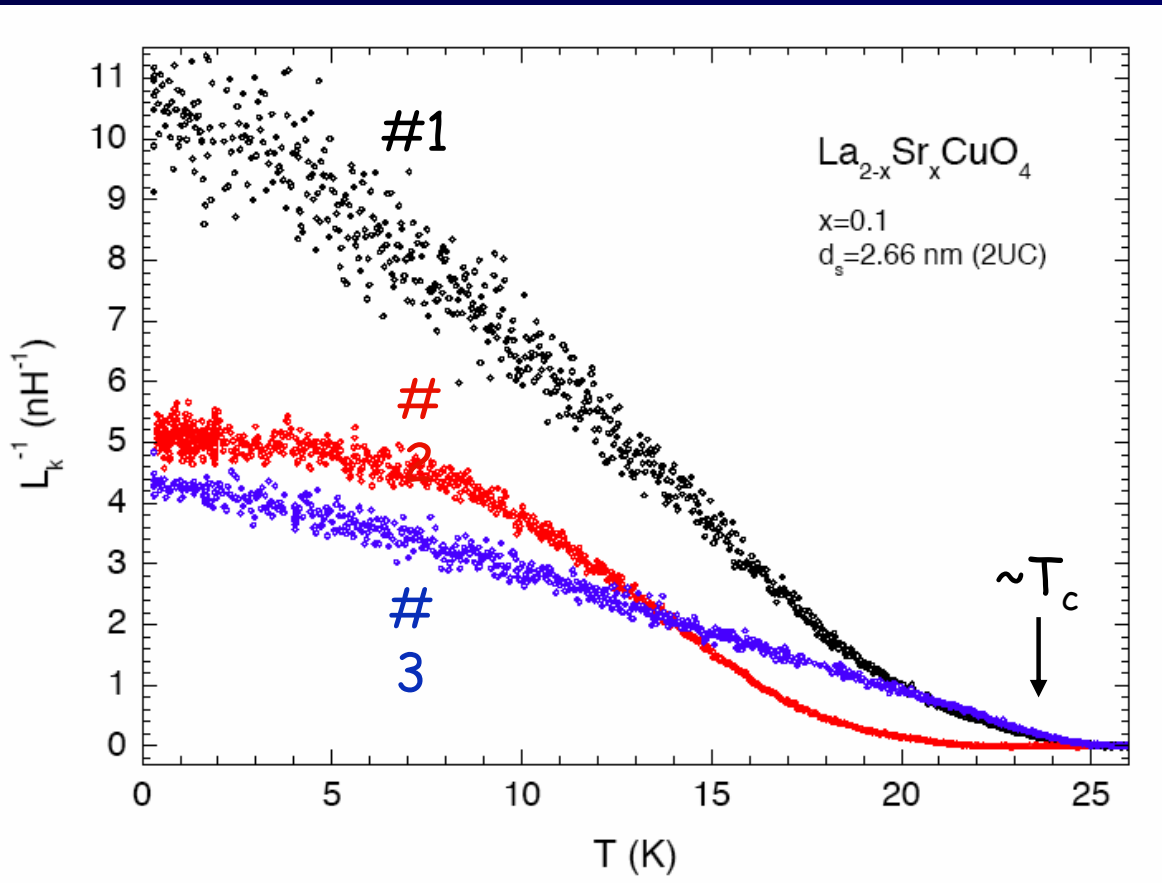
For « nodal » order parameter at $T \ll T_c$:

[G.E. Volovik, JETP Lett. (93);
S.G. Sharapov *et al.*, PRB (02)]

$$\Delta L_k^{-1}(B) \propto B^{1/2}$$

For s -wave SC : $\Delta L_k^{-1}(B) \propto B$

Effect of disorder on the superfluid response $L_k^{-1} = e^2 n_{s\Box} / m^*$



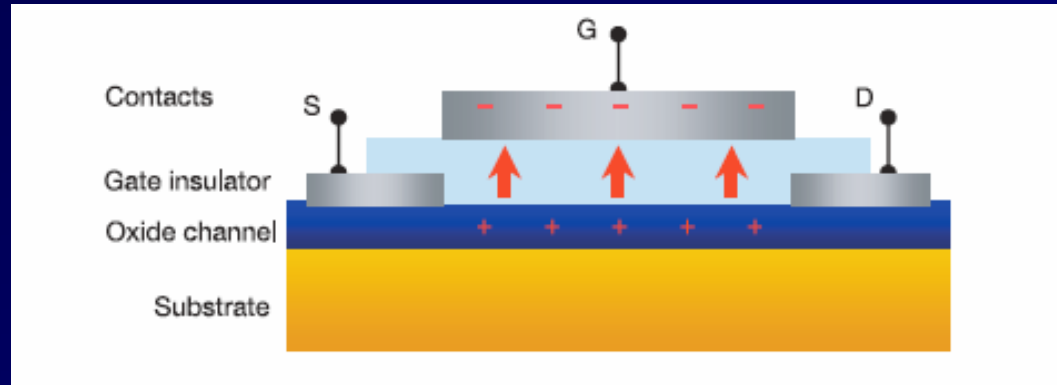
LSCO films with the same thickness ($d_s = 2$ UC) and the same doping ($x = 0.1$):

1. Have approximately the same T_c
2. But differ substantially in $L_k^{-1}(0)$

M. Franz et al., PRB (97)

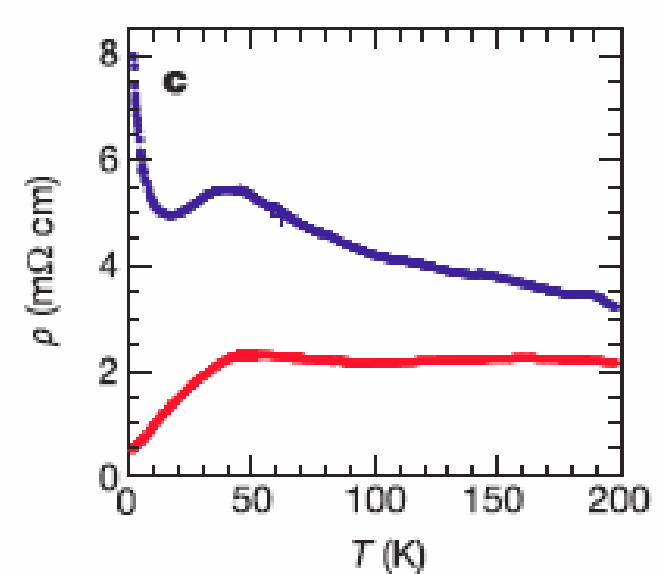
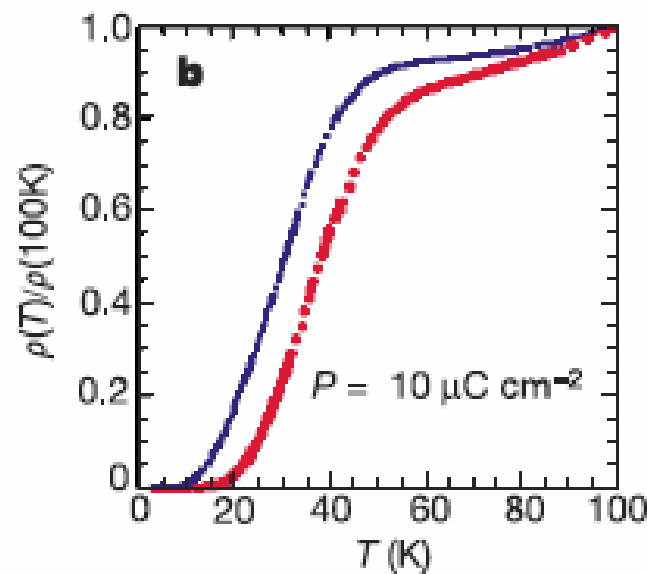
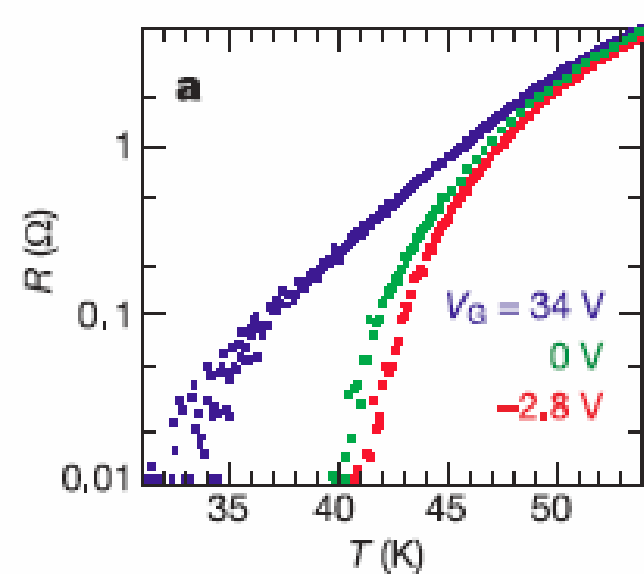
	# 1	# 2	# 3
$\tau^{-1} \times 10^{-11} [s^{-1}]$	2.0	4.1	6.0
v_F / v_Δ	37	32	25

Previous work on electrostatic modulation



Dielectric gate

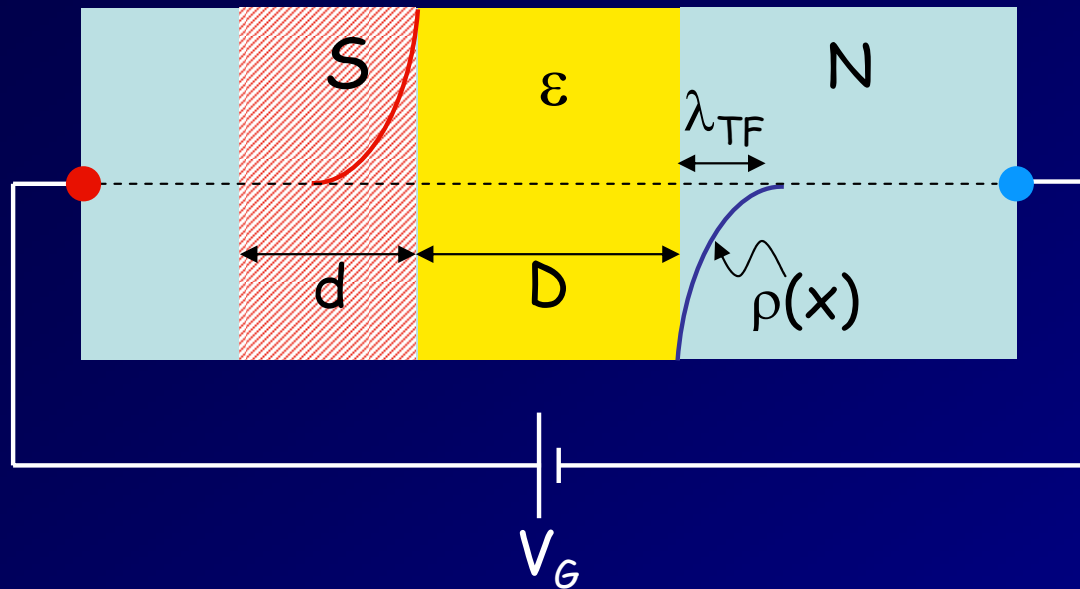
Ferroelectric (PZT) gate



J. Mannhart, *Supercond. Sci. Technol.* (1996)

C.H. Ahn *et al.*, *Science* (1999)

Electrostatic modulation of $L_k^{-1} = e^2 n_{s\Box} / m^*$



$$\begin{aligned} \Delta L_k^{-1} / L_k^{-1} &= \Delta Q_s / Q_s \\ &= (C V_G / e n_{s\Box}) [1 - \exp(-d / \lambda_{TF})] \end{aligned}$$

$$C^{-1} = C_\epsilon^{-1} + C_{TF}^{-1} = (D / \epsilon \epsilon_0) + (\lambda_{TF} / \epsilon_0)$$

$$\lambda_{TF} = (\hbar / e) [\pi \epsilon_s \epsilon_0 d / m]^{\frac{1}{2}} \approx 0.5 \text{ nm}$$

[H. Beck and D. Ariosa (95)]

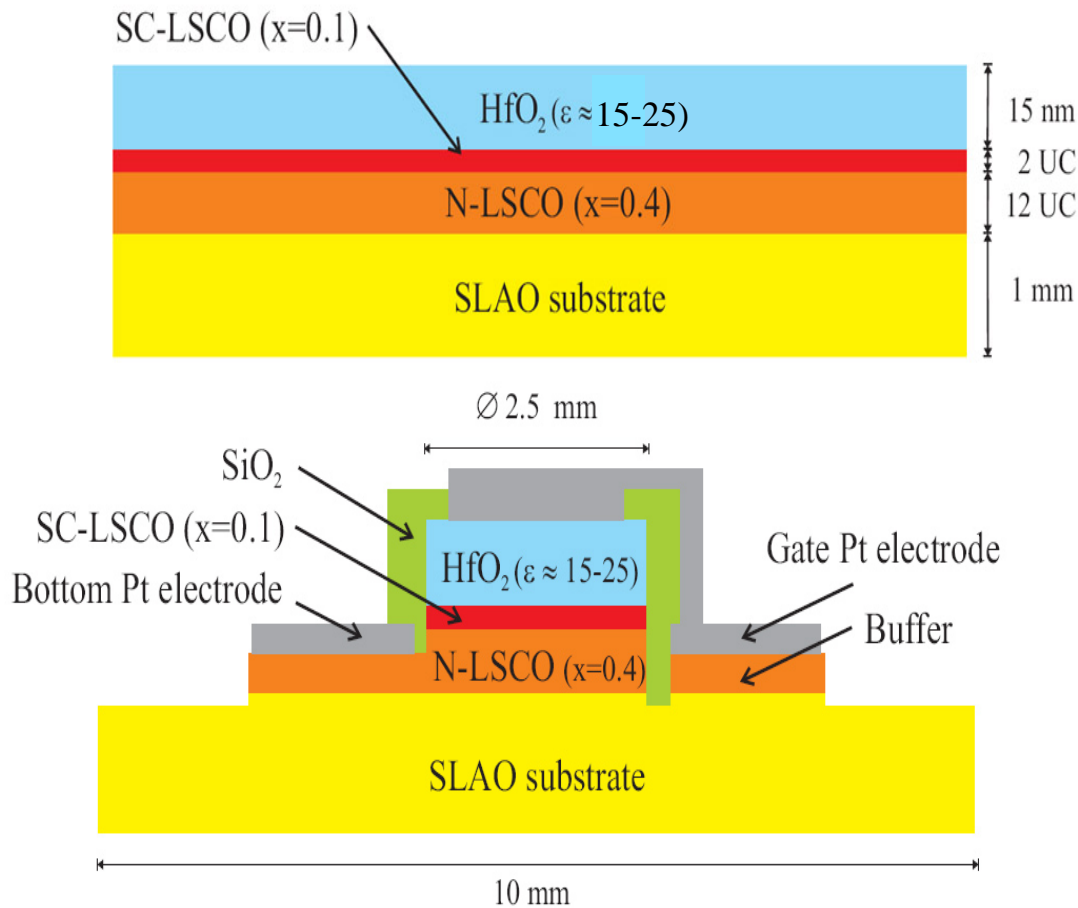
Limiting cases (for $D / \epsilon \lambda_{TF} \gg 1$, $E \equiv V_G / D$):

$$d \ll \lambda_{TF} \Rightarrow \Delta L_k^{-1} / L_k^{-1} = \epsilon \epsilon_0 E / e n_s \lambda_{TF} \quad (\text{max. modulation for } E = E_B)$$

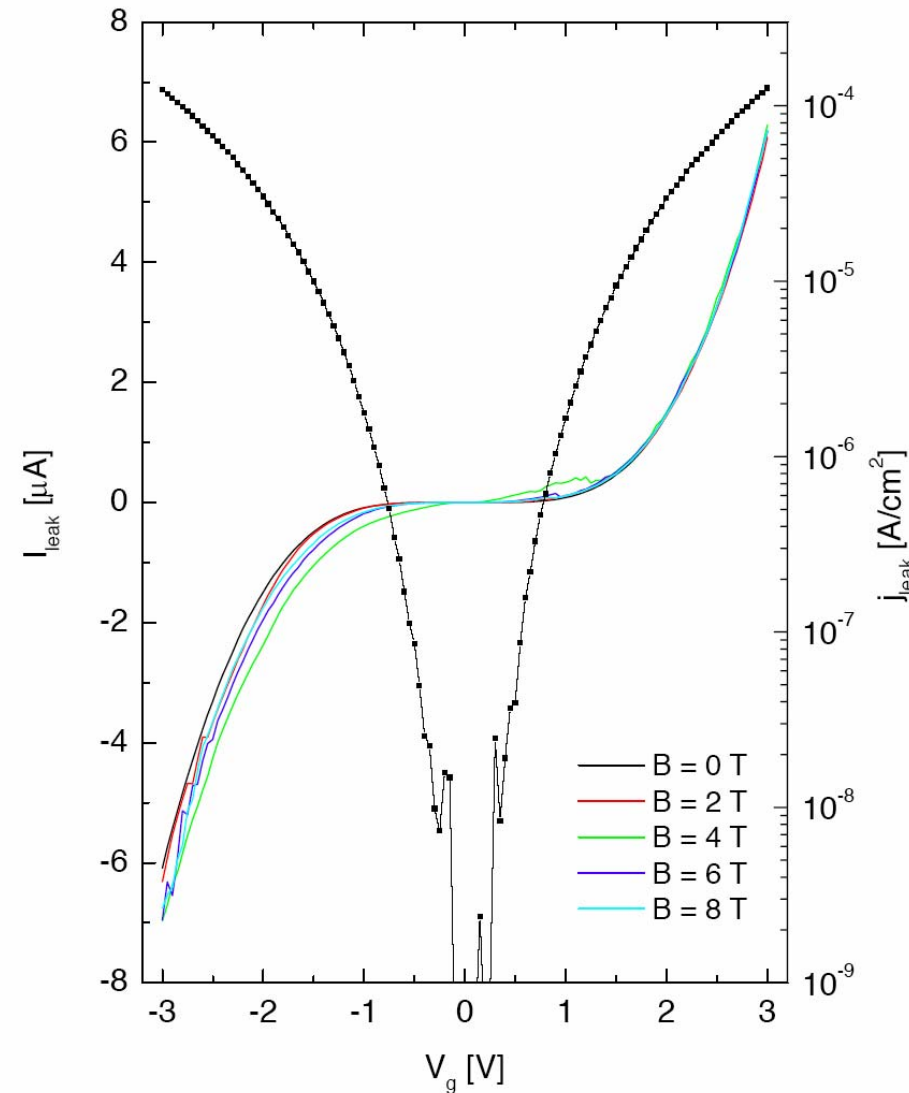
$$d \gg \lambda_{TF} \Rightarrow \Delta L_k^{-1} / L_k^{-1} = \epsilon \epsilon_0 E / e n_s d \Rightarrow \text{Ultrathin Films: } d > \lambda_{TF}$$

Fabrication of electric-field-effect heterostructures

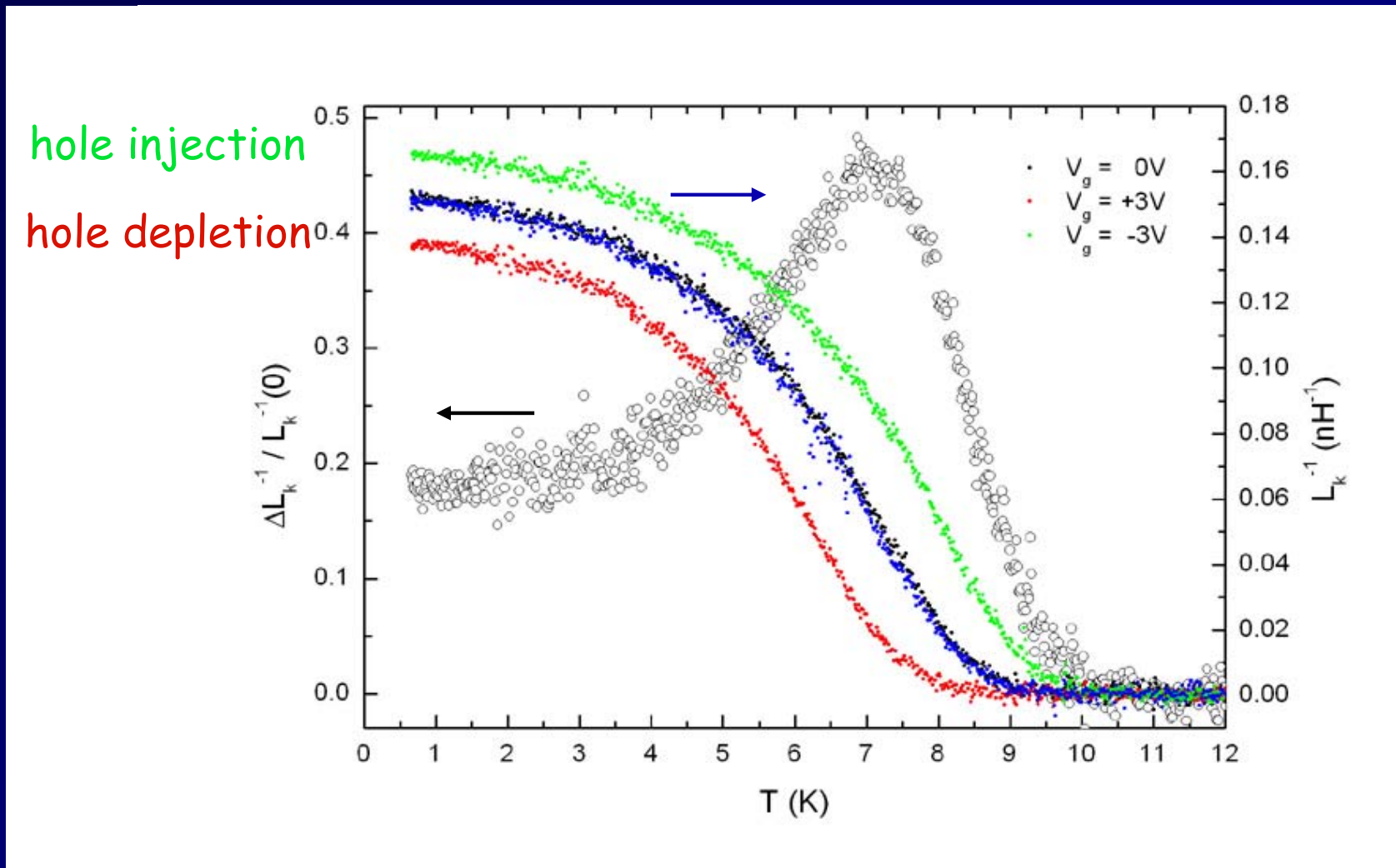
Leakage current vs V_G



$d = 2.66$ nm (2UC)



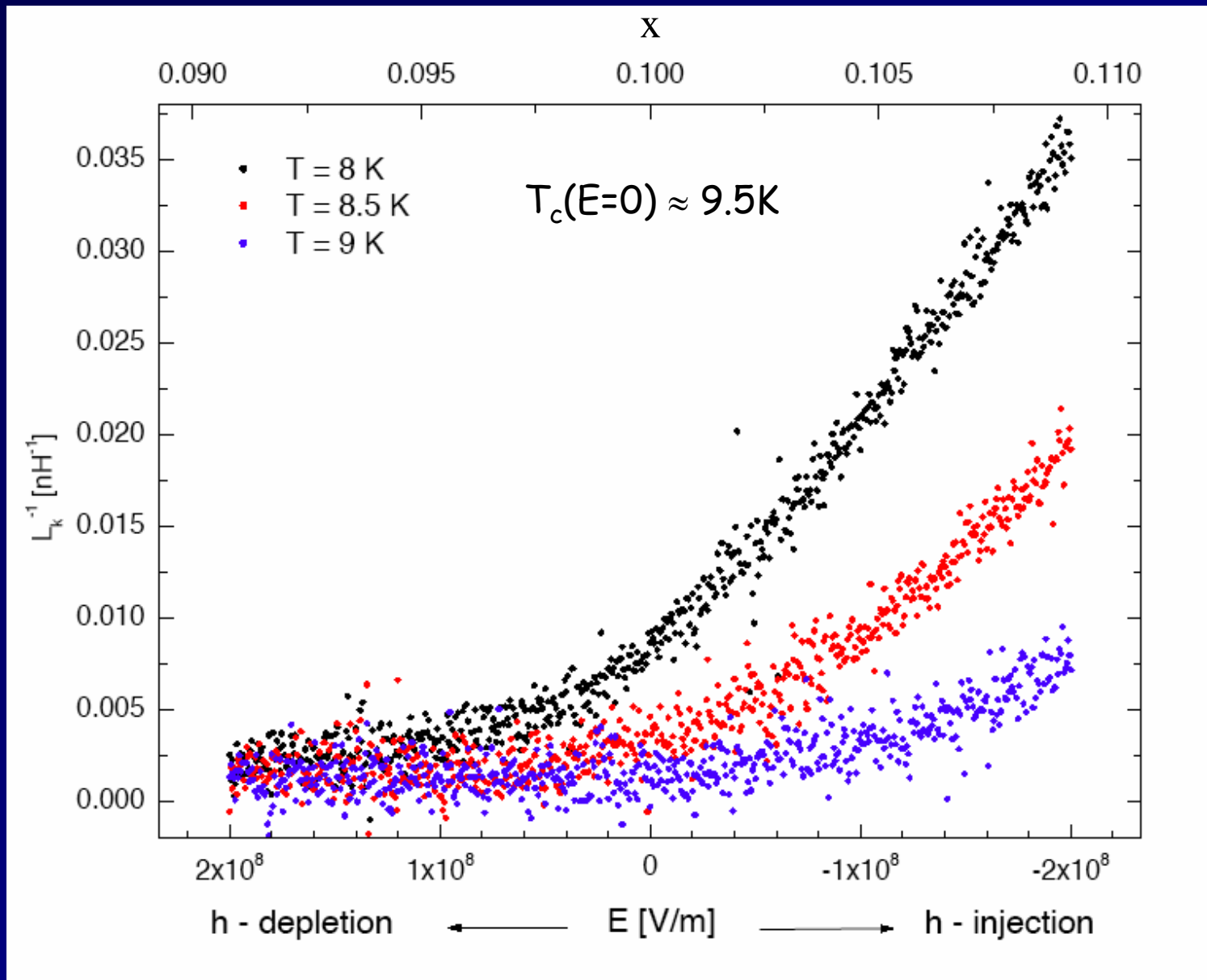
Absolute and relative electrostatic modulation of $L_k^{-1}(T)$



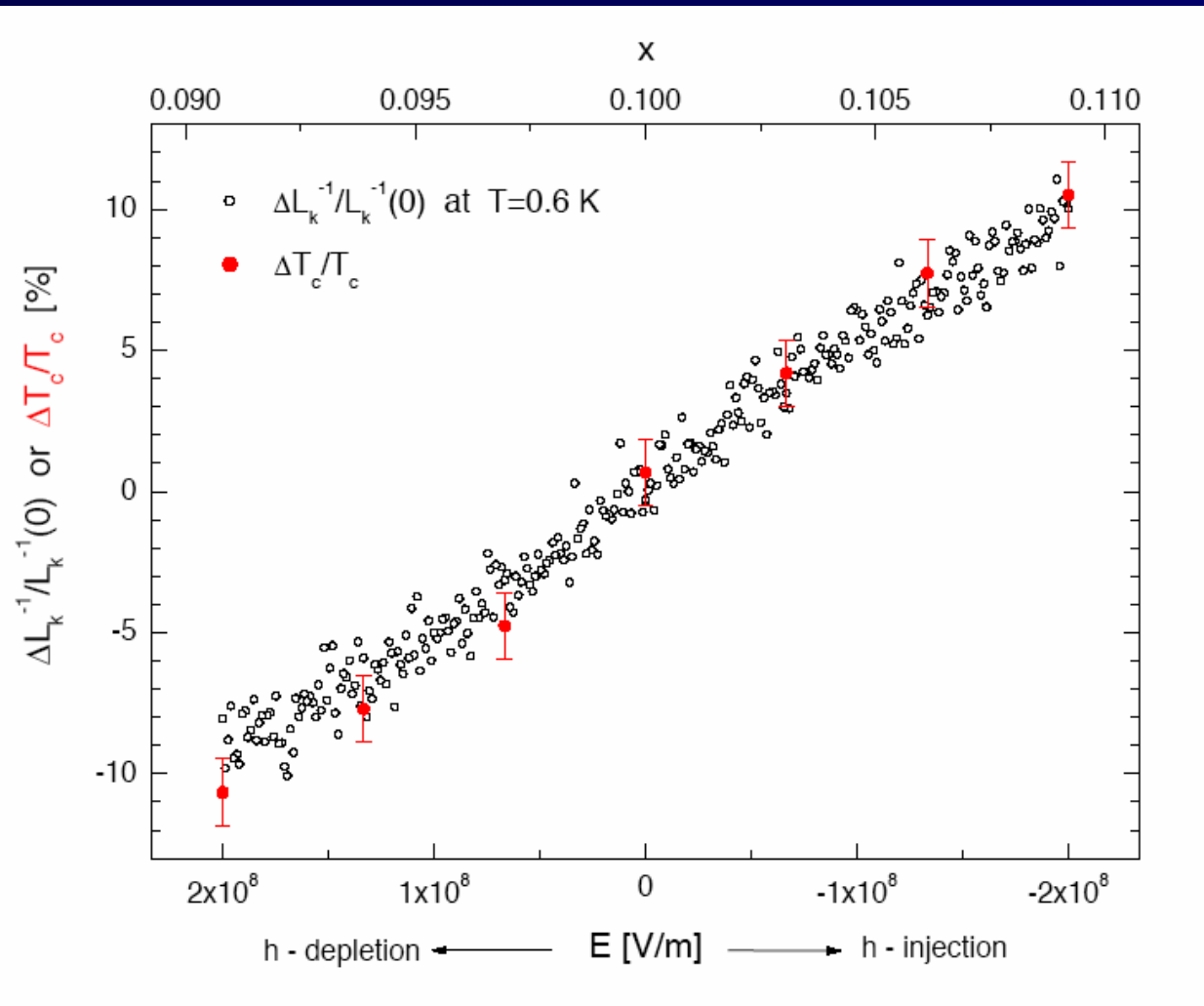
At $T = 0$: $\Delta L_k^{-1} / L_k^{-1}(0) \approx \pm 9\%$ for $E = V_g / D \approx \pm 2 \times 10^8 \text{ V/m}$

A.T. Fiory *et al.*, PRL (90) : $\Delta L_k^{-1} / L_k^{-1}(0) \approx 10^{-5}$; A.T. Findikoglu *et al.*, APL (93)

Electric-field-induced superconductivity : $L_k^{-1}(E)$ isotherms near T_c



Comparison of $\Delta T_c(E)/T_c(0)$ and $\Delta L_k^{-1}(E)/L_k^{-1}(0)$ for $T \rightarrow 0$



Unambiguous evidence for the « Uemura relation » :

$$L_k^{-1}(T=0) \propto T_c$$

In the underdoped regime
(if $\Delta n_s/n_s = \Delta n_h/n_h$) :

$$\Delta L_k^{-1}/L_k^{-1}(T=0) = \varepsilon \varepsilon_0 E / e n_h d$$

n_h = # of free holes

$$x \approx 0.1 \Leftrightarrow n_h \approx 1.05 \times 10^{21} \text{ cm}^{-3}$$



$$\varepsilon \approx 23$$

J. Robertson, Eur. Phys. J. Appl. Phys. (2004) :
 $\varepsilon \approx 25$ for HfO_2

Temperature dependence of $\Delta L_k^{-1}/L_k^{-1}(0)$

Model for the underdoped regime based on :

1. The « Uemura » relation ($T = 0$)

$$L_k^{-1}[T=0, T_c(E)] \propto T_c(E)$$

2. Factorization of temperature dependence

$$L_k^{-1}[T, T_c(E)] = L_k^{-1}[0, T_c(E)] f[T/T_c(E)]$$

Then :

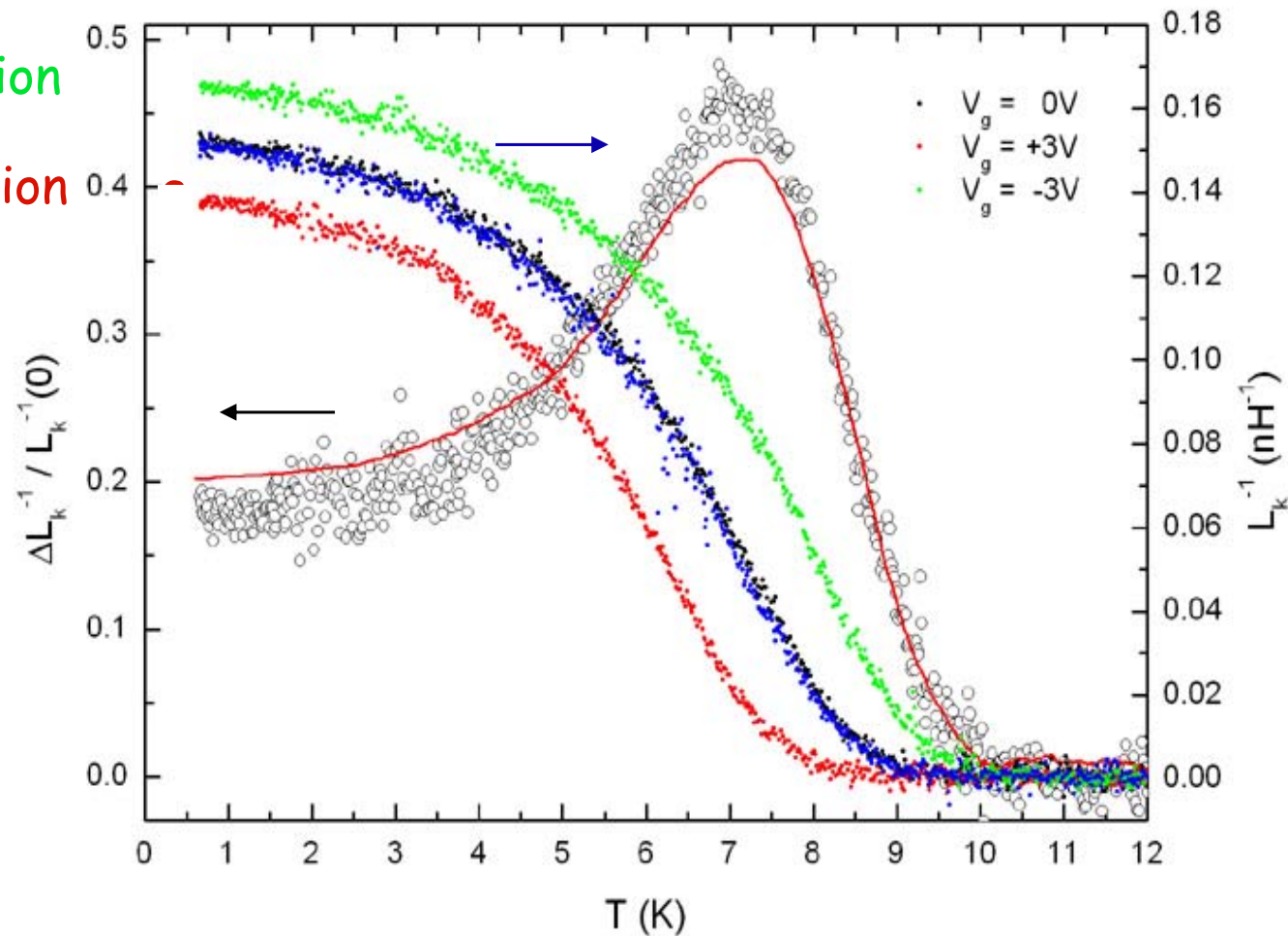
$$\Delta L_k^{-1}(T, E)/L_k^{-1}(0) = [f(T/T_c) - T(df/dT)]_{E=0} \Delta T_c(E)/T_c(0)$$

No adjustable parameters !

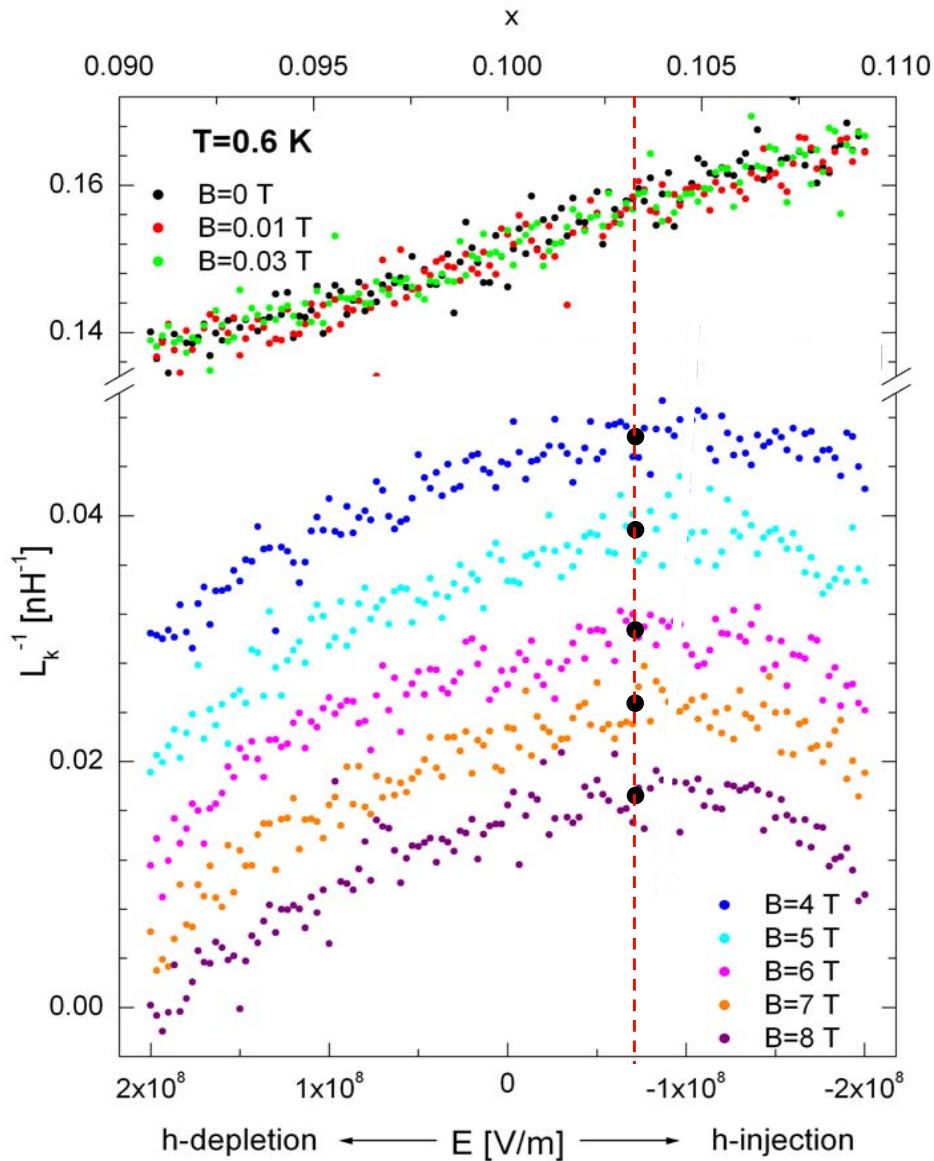
Relative electrostatic modulation $\Delta L_k^{-1}(T)/L_k^{-1}(0)$: Comparison with model calculation

hole injection

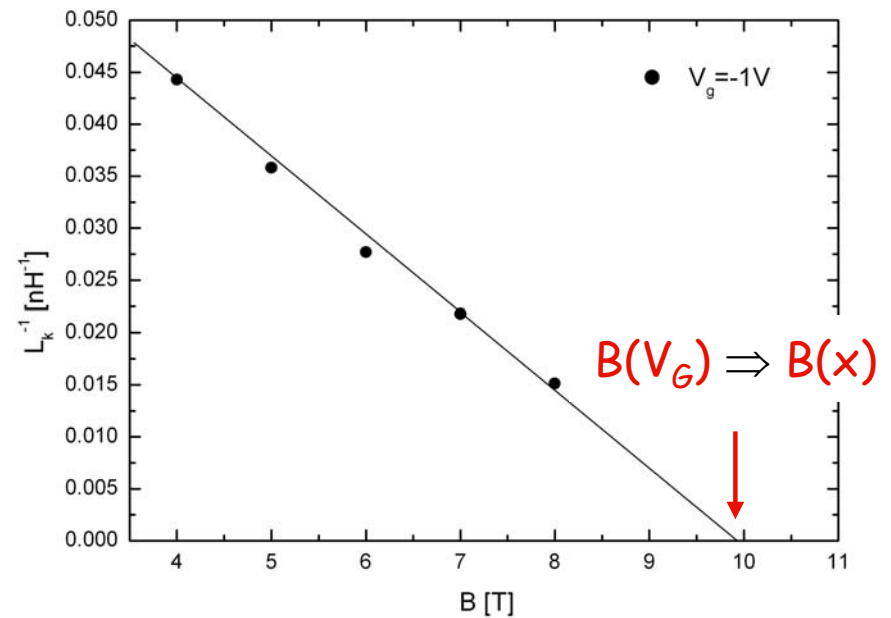
hole depletion



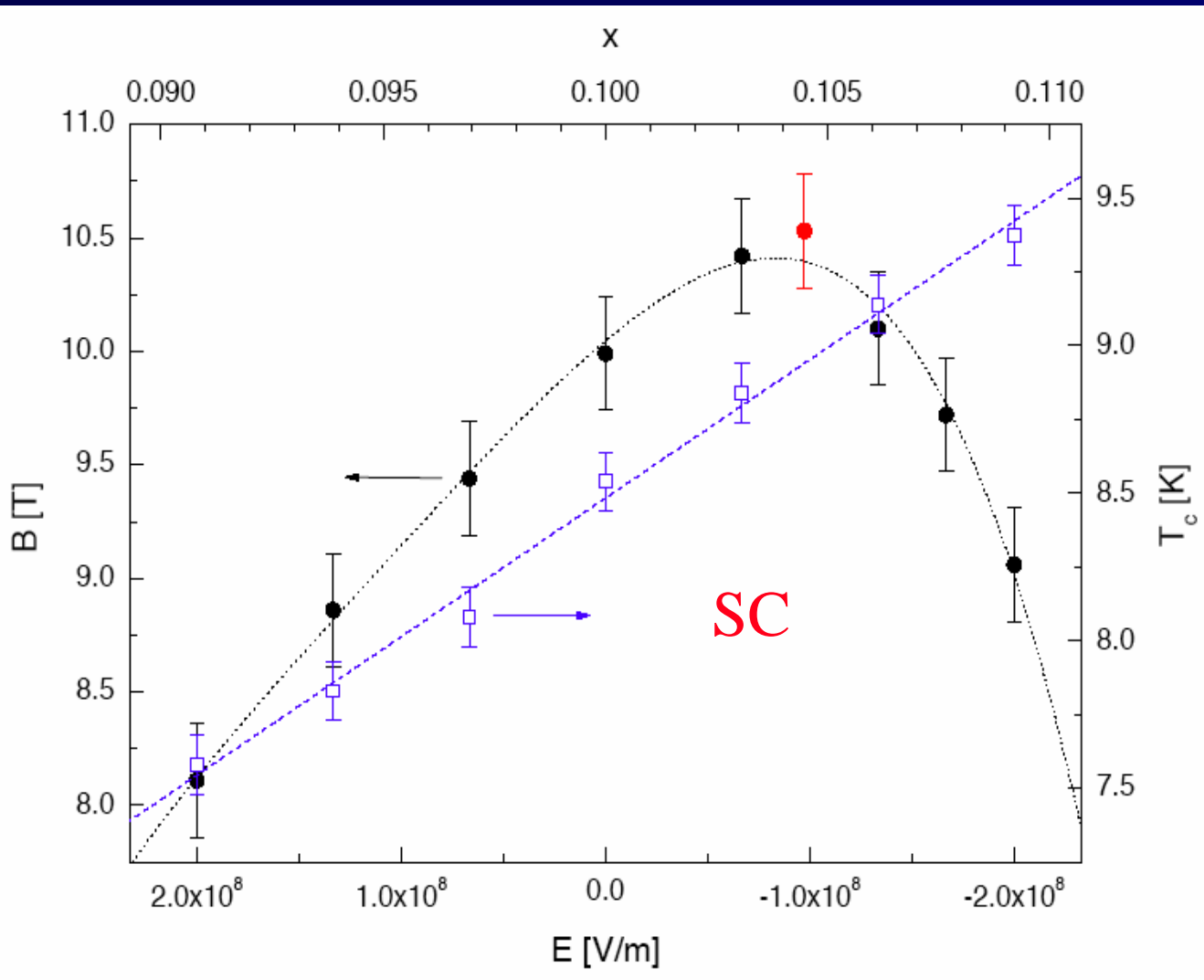
Low-temperature electrostatic modulation of L_k^{-1} in a magnetic field



Regime crossover (reentrant behavior) at high magnetic fields



Phase Diagrams : $B(T = 0)$ and T_c vs carrier concentration x



Why maximum below the $B=0$ optimum doping ($x=0.16$) ?

- 1/8-anomaly in LSCO [T_c depression at $x = 0.125$] ?
- B-induced shift of optimum doping to lower x ?
- B-dependence of ε ?

Free carrier effective mass m^*

$$m^*/m_e = (e/m_e)\epsilon\epsilon_0(\Delta V_G/D)L_{KL}(0)[\Delta L_k^{-1}/L_k^{-1}(0)]^{-1}$$

$$L_{KL}(0) \equiv \mu_0\lambda_{ab}^2(0)/d = 43.7 \text{ pH} \quad \text{using (bulk) } \lambda_{ab}(0) = 304 \text{ nm}$$

[A.J. Zaleski and J. Klamut, J. Phys.: Cond. Matt. 11, 9371 (1999)]

$$\epsilon \approx 23 \quad \Delta L_k^{-1}/L_k^{-1}(0) \approx 9\% \quad (\text{for } \Delta V_G/D = 2 \times 10^8 \text{ V/m})$$

$$m^*/m_e \approx 3.5$$

CONCLUSIONS AND OUTLOOK

1. Observation of the first large ($\sim 10\%$) electrostatic modulation of the (areal) superfluid density (magnetic penetration depth) in ultrathin films of cuprate superconductors (LSCO).
2. Compelling evidence for the validity of the « Uemura relation » [$T_c \propto \lambda_{ab}^{-2}(0)$] in the underdoped regime.
3. Observation of an intriguing regime crossover at high B-fields.

Outlook :

SC-Insulator (quantum) phase transition in the extreme underdoped regime, overdoped regime, magnetic field effects, ...